Harmonics and powers of doubly fed induction generators at balanced sinusoidal voltages

Abstract. Measurements at a test-bench of a wind energy converter performed with an ideal balanced and sinusoidal voltage source instead of a grid are necessary for the identification of the harmonics or subharmonics caused by the generator and converter. The produced significant frequencies as well as their interaction with the voltage source are analyzed. The stator side collective power components are calculated and their effect on the time variable asymmetry of the stator current of the three-phase system is investigated.

Streszczenie. Identyfikacja harmonicznych i subharmonicznych wprowadzanych przez generatory i przekształtniki energii wiatrowej wymaga pomiarów laboratoryjnych w warunkach zasilania napięciem sinusoidalnym i symetrycznym. W artykule analizowane są wytwarzane w takich układach znaczące składowe częstotliwościowe a także ich oddziaływanie na źródło zasilania. Obliczane są także składowe mocy po stronie stojącej oraz badany jest ich wpływ na czasową zmienność asymetrii prądu stojącego. (Harmoniczne i moce dwustronnie zasilanych generatorów indukcyjnych przy sinusoidalnych i symetrycznych napięciach zasilających).

Keywords: asymmetries, balanced sinusoidal voltage, DFIG, harmonics, wind turbine, power components

Stowa kluczowa: asymetrie, symetryczne napięcie sinusoidalne, DFIG, harmoniczne, turbina wiatrowa, składowe mocy.

Introduction

Wind energy converters must comply with standards like those described in EN 50160 [1] or IEC 61000 [2]. Especially harmonics can distort the grid and must not exceed the given limits. In practice harmonics or subharmonics caused by the wind turbine are difficult to measure, because the grid itself is also distorted.

Better conditions exist with a test-bench. Instead of a distorted power grid it can be operated with an ideal voltage source, which has nearly no internal impedance and gives a pure sinusoidal balanced voltage. In this way, all harmonics in the measurement arise from the doubly fed induction generator with its converters. Their propagation from rotor to stator is described in [3], which is the basis for the following explanations.

The sources of the measured harmonics are also investigated. Furthermore, the influences of harmonics and subharmonics on the power output are analysed.

I. Description of the Test-Bench

Measurements are taken with a test-bench that is shown in Fig. 1. It consists of a doubly fed induction generator (DFIG) with a back-to-back voltage source converter in the rotor circuit, a DC-machine as a model of the wind torque and an ideal voltage source instead of a grid.

The 23 kW DC-machine is separately excited. It creates the needed torque and angular velocity, which are regulated by a 4-quadrant converter. For each wind speed an optimal angular velocity with maximum mechanical power is chosen. With the controller of the DC-machine the rotation speed can be varied from the nominal value of 1500 rpm to a range of 1200-1800 rpm.

A 5 kW slip-ring induction machine with two pole pairs is used as a generator. Its stator coils are star-connected with star point not grounded; the coils of the rotor are delta-connected. The rotor is fed by a back-to-back-converter and a transformer, see Fig. 1. The filter in the rotor circuit minimizes distortion caused by the pulses of the converter.

For the measurements described in this paper the machine is operated in super-synchronous mode with a rotation speed of 1650 rpm, i.e. with a slip of −0.1 and controller set values of a collective active power of -3 kW and a symmetric 50 Hz reactive power of 0.4 kvar.

Fig. 1 shows that the grid is substituted in the test-bench by an ideal voltage source \( V_{\text{Ideal}} \) and an impedance \( Z_{\text{Grid}} \). The voltage is generated by a 4-quadrant-amplifier. It includes two oscillators, which can generate three separate phase-to-ground voltages with a maximum signal frequency of 5 kHz. The voltage harmonics of each phase and the asymmetry of the three phase system can also be set. For the described analysis a symmetrical and pure sinusoidal three-phase voltage system is used. It has a phase-to-ground voltage with an RMS-value of 230 volts and a frequency of 50 Hz, which is identical to the fundamental frequency of the grid. The three phase grid impedance \( Z_{\text{Grid}} \) for this frequency is chosen to \((0.24+0.15)\, \Omega\) in conformity with the specifications of EN 61000-3 [4].

There are four points in the test-bench, where the measurements are performed. Point A gives the voltages and currents of the stator, where the voltages are measured against its star point. At point B the rotor currents are recorded. In the measurements on the rotor side (point B) only lower harmonics up to some hundred Hz are taken into account. Higher harmonics, caused by the pulses of the converters, are neglected for this discussion. They are described e.g. in [5] and [6]. Values of powers fed into the grid from the rotor circuit are taken at point C; the voltages of the ideal source are measured at point D.

At the investigated operation point of 1650 rpm the electrical fundamental frequency \( f_{\text{er},1} \) in the rotor can be calculated by

\[
(1) \quad f_{\text{er},1} = f_{\text{s},1} - p \cdot \frac{n}{60} = 50\, \text{Hz} - 2 \cdot \frac{1650\, \text{rpm}}{60} = -5\, \text{Hz}
\]

with generator speed \( n \), pole pairs \( p \), stator fundamental frequency \( f_{\text{s},1} \) (50 Hz). This equation outlines that rotor frequencies can become very low. For this reason current transformers for a specified frequency range of 0-8000 Hz are chosen.

Fig. 1. Test-bench with ideal voltage source for measurements of voltages and currents at points A, B, C and measurements of voltages at point D
are used. Their measuring accuracy is 2 % of the upper limit of the effective range. The sampling rate of the measurements is 10 kHz, i.e. much higher than the considered harmonic frequencies.

The negative sign in (1) indicates that the fundamental frequency in the rotor has a negative sequence. Therefore, its field in the air gap rotates opposite with the field of the fundamental stator current and the mechanical speed. The frequency itself, of course, is always positive.

II. Measurement results

The measurements are performed in super-synchronous mode with a speed of 1650 rpm. At the stator of the generator (point A at Fig. 1) the voltages and currents are recorded with the same sampling rate of 10 kHz. These values are necessary for the calculation of harmonics and power components. In the same manner the voltages and currents as well as the powers in point B and C are determined. To verify the balanced pure sinusoidal 50 Hz ideal voltage source, the three phase-to-ground voltages are measured at point D. Their harmonics are calculated. In all four points the measurements were synchronized. With the help of input filters with a cut-off frequency of 5 kHz aliasing effects were avoided.

A) Harmonics in voltages and currents

First, the voltages and currents at points A and B are discussed; see Fig. 2 and Fig. 3. The calculated harmonics in these voltages and currents are shown in Table 1.

The stator voltage contains essentially a third harmonic with 150 Hz, while in the current the frequencies of 20 Hz, 80 Hz and 150 Hz are significant. In the rotor the seventh harmonic with 35 Hz is strong; further significance have the fifth, eleventh and thirteenth harmonic with 25 Hz, 55 Hz and 65 Hz. These harmonics must originate from the generator and its converters during active power feeding in the super-synchronous operating mode, because the three-phase ideal voltage source is pure sinusoidal 50 Hz and symmetric.

Fig. 4 shows the measured voltages at the ideal voltage source (point D). All magnitudes of the considered harmonic and sub harmonic frequencies are less than 0.1 % of the amplitude of the fundamental frequency. This verifies that all measured harmonics at points A, B and C originate only from the DFIG and its converters.

Table 1. Relative collective voltage and current harmonics in super-synchronous mode

<table>
<thead>
<tr>
<th>Harmonic</th>
<th>(U_{h\Sigma}^<em>), (I_{h\Sigma}^</em>)</th>
</tr>
</thead>
<tbody>
<tr>
<td>(U_A^*) (10 Hz)</td>
<td>0.02 %</td>
</tr>
<tr>
<td>(U_A^*) (20 Hz)</td>
<td>0.08 %</td>
</tr>
<tr>
<td>(U_A^*) (80 Hz)</td>
<td>0.03 %</td>
</tr>
<tr>
<td>(U_A^*) (110 Hz)</td>
<td>0.02 %</td>
</tr>
<tr>
<td>(U_A^*) (150 Hz)</td>
<td>5.36 %</td>
</tr>
<tr>
<td>(I_A^*) (10 Hz)</td>
<td>0.45 %</td>
</tr>
<tr>
<td>(I_A^*) (20 Hz)</td>
<td>7.29 %</td>
</tr>
<tr>
<td>(I_A^*) (80 Hz)</td>
<td>3.58 %</td>
</tr>
<tr>
<td>(I_A^*) (110 Hz)</td>
<td>0.37 %</td>
</tr>
<tr>
<td>(I_A^*) (150 Hz)</td>
<td>1.44 %</td>
</tr>
<tr>
<td>(I_B^*) (25 Hz)</td>
<td>0.87 %</td>
</tr>
<tr>
<td>(I_B^*) (35 Hz)</td>
<td>3.37 %</td>
</tr>
<tr>
<td>(I_B^*) (55 Hz)</td>
<td>0.92 %</td>
</tr>
<tr>
<td>(I_B^*) (65 Hz)</td>
<td>0.50 %</td>
</tr>
<tr>
<td>(I_B^*) (95 Hz)</td>
<td>0.16 %</td>
</tr>
</tbody>
</table>

The harmonics of ordinal number \(h\) are calculated as collective root-mean square-value \(I_{h\Sigma}\) of the corresponding frequency in the three phases:

\[
I_{h\Sigma} = \sqrt{\frac{3}{\sum_{l=1}^{3} I_{hl}^2}}.
\]

The resulting values are normalized with the collective root-mean square-value \(I_{1\Sigma}\) of the three-phase fundamental current:

\[
I_{h\Sigma}^* = \frac{I_{h\Sigma}}{I_{1\Sigma}} \cdot 100\%,
\]

where \(I_{1\Sigma}, I_{1\Sigma}\) equal 7.52 A and 12.56 A respectively. The same procedure is applied for the star-voltages, in which case the collective voltage \(U_{1\Sigma}\) has a value of 402.5 V. The root-mean-square-values are averaged over ten times the fundamental period.

The stator voltage contains essentially a third harmonic with 150 Hz, while in the current the frequencies of 20 Hz, 80 Hz and 150 Hz are significant. In the rotor the seventh harmonic with 35 Hz is strong; further significance have the fifth, eleventh and thirteenth harmonic with 25 Hz, 55 Hz and 65 Hz. These harmonics must originate from the generator and its converters during active power feeding in the super-synchronous operating mode, because the three-phase ideal voltage source is pure sinusoidal 50 Hz and symmetric.

Fig. 4 shows the measured voltages at the ideal voltage source (point D). All magnitudes of the considered harmonic and sub harmonic frequencies are less than 0.1 % of the amplitude of the fundamental frequency. This verifies that all measured harmonics at points A, B and C originate only from the DFIG and its converters.
Besides harmonics, Fig. 2 reveals another effect. The stator currents have a significant asymmetry. Furthermore, this asymmetry is not static, but changing with time. In Fig. 2 the alternating averaging rms-values of the phase currents at point A verify this statement. The described effect cannot be caused by the construction of the machine. Tests showed that the machine itself has only negligible asymmetries. Furthermore, if the machine construction was the cause, the asymmetries would be static.

The reason for this effect is the strong 20-Hz-frequency in the stator currents. This low frequency varies the currents with a shape, which repeats every 100 ms, because 20 Hz is no divisor of 50 Hz.

This effect differs in the three phases; therefore the current amplitudes are also different, seeming to be an asymmetry. This asymmetry varies about 100 ms. So the currents can show asymmetric amplitudes, although everything is symmetrical in itself. In Fig. 5 the time curves of the stator currents demonstrate this effect of the 20 Hz component considered, exemplarily at phase L1. For reference the fundamental component is also illustrated. The calculation of harmonics in time domain is described in [3]. The sum of the 20 Hz and 50 Hz components characterise substantially the time curve of the respective stator phase current.

The fluctuating currents are difficult to control and are a challenge for the controller concept. Moreover, these fluctuations have also an impact on the power components of the generator.

### B) Asymmetries in stator currents

**Fig. 4.** Measured values of the three-phase ideal voltage source at point D during active power feeding in super-synchronous mode (time curves and the corresponding harmonics)

Seeking the reason for the additional frequencies at measurement points A and B, let’s at first have a look at the rotor circuit. The rotor side converter works as a 6-pulse double bridge rectifier. This device causes current harmonics with ordinal numbers of k:

\[ k = 1 + 6 \cdot g \quad \text{with} \quad g = 0, \pm 1, \pm 2, \ldots \]

Hence, significant values of k are –5, +7, –11 and +13. Because the fundamental rotor frequency is a negative sequence of 5 Hz, the corresponding rotor harmonics are +25 Hz, –35 Hz, +55 Hz and –65 Hz. According to the explanations in [3], these harmonics correspond to stator current frequencies of 80 Hz, 20 Hz, 110 Hz and 10 Hz. Thus the strongest harmonics of 20 Hz and 80 Hz in the stator current (7.29 % and 3.58 %) arise from the seventh and fifth harmonic in the rotor current, caused by the rotorside converter.

These stator current harmonics occur also in the voltage of the stator, although the voltage source is pure sinusoidal. The reason is that the current creates a voltage drop at the grid impedance \( Z_{\text{grid}} \), which is proportional to the current. In that way, the harmonics of the currents couple to the voltages of the stator.

Still not discussed is the third harmonic with 150 Hz in the stator voltage. It is a consequence of the nonlinear magnetisation characteristic of the iron core. For the magnetisation a third harmonic is needed. If the star point is magnetisation a third harmonic is needed. If the star point is not connected. But if you excite an iron core e.g. with a sinusoidal current, the third harmonic will occur in the voltage, however inverse to the third current harmonic. As the measurements show, this 150-Hz-component is a pure zero sequence.

Nevertheless, the stator currents contain also a 150-Hz-harmonic. This component is composed of a positive and a negative sequence. According to [3] and [7] the positive sequence corresponds to a rotor frequency of 95 Hz, which has a value of 0.16 %. The negative sequence creates a rotor harmonic of 205 Hz that exceeds the range of Table 1.

**Fig. 5.** Time curves of the stator current L1 at measurement point A, consisting of the 50 Hz and 20 Hz components exclusively

This effect is the strong 20-Hz-frequency in the stator currents. This low frequency varies the currents with a shape, which repeats every 100 ms, because 20 Hz is no divisor of 50 Hz.

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### C) Influences of Stator Harmonics on Powers

The power output is calculated by the measured voltages and currents at the stator (point A) and at the converter-transformer (point C), where the rotor power is fed in. At first, the instantaneous collective power \( P_{\text{coll,inst}} \) of the three phases is determined by using the equation:

\[
P_{\text{coll,inst}}(t) = \sum_{i=1}^{3} P_{i,\text{inst}}(t) = \sum_{i=1}^{3} v_i(t) \cdot i_i(t),
\]

where \( P_{i,\text{inst}}(t) \) is the instantaneous power of phase \( i \), which can be written as a product of the respective values of the phase-to-neutral voltage \( v_i(t) \) and the phase current \( i_i(t) \). The instantaneous collective powers \( P_{\text{coll,inst}} \) of all three phases at these two points as well as the sum \( P_{\Sigma,\text{coll,inst}}(t) \) of both are shown in Fig. 6.

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**Fig. 4.** Measured values of the three-phase ideal voltage source at point D during active power feeding in super-synchronous mode (time curves and the corresponding harmonics)

**Fig. 5.** Time curves of the stator current L1 at measurement point A, consisting of the 50 Hz and 20 Hz components exclusively
The time curves of these collective power components are shown in Fig. 7. $S_{A, coll,T1}$ is composed of the single values from $S_{A, coll}$ for every respective fundamental term T1 within the total time interval. The apparent power curve $S_{A, coll,T1}$ is not constant over the entire time interval, it oscillates around the constant apparent power $S_{A, coll, tot} = 3.034$ kVA, which is taken over 0.2 sec. This effect is caused by the non-static collective active power $P_{A, coll}$ and the time variation of the collective non-active power component $Q_{A, coll}$.

Fig. 7. Collective power components at measurement point A with respect to time

For a better comparison, in Fig. 7 the absolute values of both time curves $P_{A, coll,T1}$ and $P_{A, coll}$ of the collective active power component are shown. The active power curve of the composed single values of $|P_{A, coll,T1}|$ varies strongly within a power range of 2.83 kW and 3.16 kW. The second curve $|P_{A, coll}|$ with a constant value of 3.006 kW is approximately equal to the absolute set value of $(\lvert 3 \rvert 3$ kW) for the controller of the collective active power.

In a further step, the collective non-active power curves at stator side are investigated. The curve of the collective non-active power $Q_{A, coll,T1}$ varies, too. There is an oscillation within the range of 0.32 kvar to 0.46 kvar, while the controller has a set value of 0.4 kvar for the symmetric 50 Hz reactive power. This fact shows that the fluctuations, caused by the 20 Hz frequency of the stator current, are significantly higher in the collective active power than in the collective non-active power.

Next the collective non-active power $Q_{A, coll,T1}$ is split up into a proportional component $Q_{A, coll,T1}$ and an orthogonal component $Q_{A, coll,T1}$. The proportional component is calculated in each of the three phases with that part of the non-active current, which is proportional to the respective phase voltage. From the RMS-values of these currents $I_{1,u}$ the collective proportional current $I_{coll,T1,u}$ results:

\[
I_{coll,T1,u} = \frac{3}{\sqrt{1}} \sum_{i=1}^{T} I_{1,u} \int_{0}^{T} v_{i}(t) \cdot i_{i}(t) \, dt
\]

The time curves of these collective power components are shown in Fig. 7. $S_{A, coll,T1}$ is composed of the single values from $S_{A, coll}$ for every respective fundamental term T1 within the total time interval. The apparent power curve $S_{A, coll,T1}$ is not constant over the entire time interval, it oscillates around the constant apparent power $S_{A, coll, tot} = 3.034$ kVA, which is taken over 0.2 sec. This effect is caused by the non-static collective active power $P_{A, coll}$ and the time variation of the collective non-active power component $Q_{A, coll}$.

Fig. 6. Time curves of instantaneous collective power at measurement points A, C and the sum of both

The collective power curves contain additional frequencies. Particularly, the power curves have a characteristic that repeats also every 100 ms. This fact shows that even the power curves are strongly influenced by the 20-Hz-component of the stator current and voltage.

The components of the stator power at measurement point A, which is dominant in the used operation point, are further investigated.

### III. Collective power components of the stator

For the calculation of the collective power components DIN EN 40110-2 is applied \[8\]. Three components of collective power are investigated: the apparent power $S_{A, coll}$ of the three-phase system, the collective active power $P_{A, coll}$ and the collective non-active component $Q_{A, coll}$.

At first, the apparent power $S_{A, coll}$ of the stator is calculated:

\[
S_{A, coll} = U_{A, coll} \cdot I_{A, coll}
\]

In (6) the collective rms-values of voltage $U_{A, coll}$ and current $I_{A, coll}$ of the three-phase system are given by:

\[
U_{A, coll} = \sqrt{\frac{1}{3} \sum_{i=1}^{3} U_{i}^2} \quad I_{A, coll} = \sqrt{\frac{1}{3} \sum_{i=1}^{3} I_{i}^2}
\]

In this context, $U_{i,j}$ and $I_{i,j}$ are the phase RMS-values.

In our investigation these rms-values are calculated over two different time periods $T$: the fundamental term $T1 = 0.02$ sec and the total interval of ten times $T1$ (tot), which is equal to 0.2 sec and represents the entire considered time interval.

Next the stator side collective active power $P_{A, coll}$ is determined by using the following equation:

\[
P_{A, coll} = \sum_{i=1}^{3} P_{i}(t) = \sum_{i=1}^{3} \frac{1}{T} \int_{0}^{T} v_{i}(t) \cdot i_{i}(t) \, dt
\]

$P_{A, coll}$ represents the balanced active power of a three-phase system over a considered time interval $T$. At last the collective non-active power $Q_{A, coll}$ is investigated, which is given by:

\[
Q_{A, coll} = \sqrt{S_{A, coll}^2 - P_{A, coll}^2}
\]
components can be less or greater than zero within every interval $T_1$.

The remaining part of the non-active current is the orthogonal component $Q_{A,coll,T_1\perp}$. It consists of reactive power and distortion components. The time curves of the collective non-active power $Q_{A,coll,T_1}$ and its components are shown in Fig. 8. These values are calculated over the fundamental period of 0.02 sec. Both the collective orthogonal part and the proportional component of the non-active power vary over the total time interval. The fluctuations of $Q_{A,coll,T_1\perp}$ are stronger than those of $Q_{A,coll,T_1\parallel u}$. This effect is caused by the 20 Hz stator current, which shapes the non-static asymmetry.

At the stator side a non static asymmetry at the currents can be observed. The analysis of the stator current harmonics shows a dominant 20-Hz-component, which originates from the propagation of the seventh current harmonics from the rotor side.

Furthermore it is observed that the 20-Hz-components of the stator currents and voltages have also an impact on the collective power curves. The power components, which are calculated over the fundamental period, are not constant over the entire time interval. This effect, though, is much higher at the collective active power than at the collective non-active power.

The described effects have been measured on a test-bench with a 5-kW-generator. They are also valid for high-power wind turbines, because the used theory of harmonics propagation from rotor to stator does not depend on the rated power of the machine.

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