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Outage probability of the SSC/SC combiner at two time instants in the presence of lognormal fading

Abstract. The outage probability of the Switch and Stay Combining/Selection Combining (SSC/SC) combiner output signal at two time instants, in the presence of log-normal fading, is determined in this paper. The probability density function (PDF) of the combiner output signal is derived. Then, the outage probability is numerically calculated using this PDF. The results are shown graphically to compare performances of the SSC/SC combiner with regard to classical SSC and SC combiners at one time instant.

Streszczenie. W artykule analizuje się prawdopodobieństwo przerw połączenia SSC/SC w obecności zaników o rozkładzie logarytmicznonormalnym. Prawdopodobieństwo to jest liczone na podstawie krzywej gęstości prawdopodobieństwa PDF. Porównano połączenia SSC/SC z klasycznymi SSC i SC. (**Prawdopodobieństwo przerw połączenia SSC/SC w obecności zaników o rozkładzie logarytmiczno-normalnym**)

Keywords: lognormal fading, SSC Combining, SC combining, two time Instants, outage probability Słowa kluczowe: zaniki połączenia, prawdopodobieństwo.

Introduction

In wireless communications, a variation of an instantaneous value of the received signal, i.e. fading of signal envelope is very common effect, due to the multipath propagation. Fading is one of the main causes of performance degradation of the receiver. Diversity technique is certainly one of the most frequently used methods for combating the deleterious effect of channel fading. Particular diversity methods and combining techniques are presented in [1].

Since the selection combining (SC) and switch and stay combining (SSC) do not require signal cophasing and fading envelope estimation, they are very often implemented in practice. The SC is combining technique where the strongest signal is chosen among L branches of diversity system [1]. In the case of dual branch SSC, the first branch stay selected as long as its instantaneous signal-to-noise ratio (SNR) is greater than predetermined switching threshold, even if the instantaneous SNR in the second branch maybe has a larger value at that time [1, 2].

The consideration of SSC systems in the literature has been restricted to low-complexity mobile units where the number of diversity antennas is typically limited to two ([3], [4], [5]). In the paper [5] Alouini and Simon develop, analyze and optimize a simple form of dual-branch switch and stay combining (SSC).

The probability density function (PDF) of the SSC combiner output signal at one time instant and the joint probability density function of the SSC combiner output signal at two time instants in the presence of Rayleigh, Nakagami-m, Weibull and lognormal fading are determined in [7-10], respectively. The probability density function and the outage probability of the SSC/SC combiner output signal at two time instants in the presence of Rayleigh fading is determined in [11].

In this paper the probability density function and the outage probability of the SSC/SC combiner output signal at two time instants in the presence of lognormal fading will be determined.

The remainder of this paper is organized as follows. The next section presents the system model and determines the probability density function, the joint PDF and the outage probability for the SSC/SC combiner output signal at two time instants. Sections III presents the numerical results obtained for performances introduced in section II. Finally, the main results of the paper are given as conclusions.

System model

The model of the SSC/SC combiner with two inputs at two time instants, considering in this paper, is shown in Figure 1. The SSC combiner input signals are r_{11} and r_{21} at first time moment and they are r_{12} and r_{22} at the second time moment. The output signals from SSC part are r_1 and r_2 . The indexes for the input signals are: first index is the ordinal branch number and the other signs time instant observed. For the output signals, the index represents the time instant observed. So found SSC combiner output signals r_1 and r_2 become the inputs in SC combiner. The overall output signal from the entire system is r.



Fig.1. Model of the SSC/SC combiner with two inputs at two time instants

The probability densities of the combiner input signals, r_{1i} and r_{2i} in the presence of log-normal fading, are [1]:

(1)
$$p_{r_1}(r_{1i}) = \frac{1}{\sqrt{2\pi\sigma_1}r_{1i}}e^{-\frac{(\ln r_{1i}-\mu_1)^2}{2\sigma_1^2}}, \quad r_{1i} \ge 0$$

(2) $p_{r_2}(r_{2i}) = \frac{1}{\sqrt{2\pi\sigma_2}r_{2i}}e^{-\frac{(\ln r_{2i}-\mu_2)^2}{2\sigma_2^2}}, \quad r_{2i} \ge 0$

where *i*=1,2, μ_i is mean value and σ_i is standard deviation of log-normal fading.

The probability of the event that combiner first examines the signal at the first input is P_1 , and for the second input is P_2 . The first case is: $r_1 < r_T$ and $r_2 < r_T$. In this case all signals at the input are below r_T , i.e.: $r_{11} < r_T$, $r_{12} < r_T$, $r_{21} < r_T$ and $r_{22} < r_T$. Let the SSC combiner first examines the signal r_{11} . Because $r_{11} < r_T$, it follows that $r_1 = r_{21}$, and since $r_{22} < r_T$ it is $r_2 = r_{12}$. The probability of this event is P_1 . When SSC combiner first examines the signal r_{21} , then $r_1 = r_{11}$ because $r_{21} < r_T$. Since $r_{12} < r_T$, then it is $r_2 = r_{22}$. The probability of this event is P_2 . After the previous, the joint probability density of the SSC combiner output signals at two time instants, r_1 and r_2 , is [10]: For $r_1 < r_T$ and $r_2 < r_T$

$$p_{r_{1}r_{2}}(r_{1}, r_{2}) = P_{1} \cdot \int_{0}^{r_{T}} dr_{11} \int_{0}^{r_{T}} dr_{22} p_{r_{11}r_{22}r_{21}r_{12}}(r_{11}, r_{22}, r_{1}, r_{2}) + P_{2} \cdot \int_{0}^{r_{T}} dr_{21} \int_{0}^{r_{T}} dr_{12} p_{r_{21}r_{12}r_{11}r_{22}}(r_{21}, r_{12}, r_{1}, r_{2})$$
(2)

(3)

For $r_1 < r_T$ and $r_2 \ge r_T$

$$p_{r_{1}r_{2}}(r_{1}, r_{2}) = P_{1} \cdot \int_{0}^{r_{T}} dr_{12} p_{r_{12}r_{11}r_{22}}(r_{12}, r_{1}, r_{2}) + P_{1} \cdot \int_{0}^{r_{T}} dr_{11} \int_{0}^{r_{T}} dr_{22} p_{r_{11}r_{22}r_{21}r_{12}}(r_{11}, r_{22}, r_{1}, r_{2}) + P_{2} \cdot \int_{0}^{r_{T}} dr_{22} p_{r_{22}r_{21}r_{12}}(r_{22}, r_{1}, r_{2}) + P_{2} \cdot \int_{0}^{r_{T}} dr_{21} \int_{0}^{r_{T}} dr_{12} p_{r_{21}r_{12}r_{11}r_{22}}(r_{21}, r_{12}, r_{1}, r_{2})$$
(4)

(4)

For $r_1 \ge r_T$ and $r_2 < r_T$

$$p_{r_{1}r_{2}}(r_{1}, r_{2}) = P_{1} \cdot \int_{0}^{r_{T}} dr_{11} p_{r_{11}r_{21}r_{22}}(r_{11}, r_{1}, r_{2}) + P_{1} \cdot \int_{0}^{r_{T}} dr_{11} \int_{0}^{r_{T}} dr_{22} p_{r_{11}r_{22}r_{21}r_{12}}(r_{11}, r_{22}, r_{1}, r_{2}) + P_{2} \cdot \int_{0}^{r_{T}} dr_{21} p_{r_{21}r_{11}r_{12}}(r_{21}, r_{1}, r_{2}) + P_{2} \cdot \int_{0}^{r_{T}} dr_{21} \int_{0}^{r_{T}} dr_{12} p_{r_{21}r_{12}r_{11}r_{22}}(r_{21}, r_{12}, r_{1}, r_{2})$$
(5)

(5)

For $r_1 \ge r_T$ and $r_2 \ge r_T$

$$p_{r_{1}r_{2}}(r_{1}, r_{2}) = P_{1} \cdot p_{r_{11}r_{12}}(r_{1}, r_{2}) + + P_{1} \cdot \int_{0}^{r_{T}} dr_{12} p_{r_{12}r_{11}r_{22}}(r_{12}, r_{1}, r_{2}) + + P_{1} \cdot \int_{0}^{r_{T}} dr_{11} p_{r_{11}r_{21}r_{22}}(r_{11}, r_{1}, r_{2}) + + P_{1} \cdot \int_{0}^{r_{T}} dr_{11} \int_{0}^{r_{T}} dr_{22} p_{r_{11}r_{22}r_{21}r_{12}}(r_{11}, r_{22}, r_{1}, r_{2}) + + P_{2} \cdot p_{r_{21}r_{22}}(r_{1}, r_{2}) + + P_{2} \cdot \int_{0}^{r_{T}} dr_{22} p_{r_{22}r_{21}r_{12}}(r_{22}, r_{1}, r_{2}) + + P_{2} \cdot \int_{0}^{r_{T}} dr_{22} p_{r_{22}r_{21}r_{12}}(r_{22}, r_{1}, r_{2}) +$$

$$+ P_{2} \cdot \int_{0}^{r_{T}} dr_{21} p_{r_{21}r_{11}r_{12}}(r_{21}, r_{1}, r_{2}) + P_{2} \cdot \int_{0}^{r_{T}} dr_{21} \int_{0}^{r_{T}} dr_{12} p_{r_{21}r_{12}r_{11}r_{22}}(r_{21}, r_{12}, r_{1}, r_{2})$$

(6)

The probabilities P_1 and P_2 are [10]:

(7)
$$P_{i} = \frac{\frac{1}{2} + erf\left(\frac{\ln r_{T} - \mu_{j}}{\sigma_{j}\sqrt{2}}\right)}{1 + erf\left(\frac{\ln r_{T} - \mu_{i}}{\sigma_{i}\sqrt{2}}\right) + erf\left(\frac{\ln r_{T} - \mu_{j}}{\sigma_{j}\sqrt{2}}\right)}$$

where *i,j*=1,2; *i*≠j.

The joint probability density function of correlated signals r_1 and r_2 with lognormal distribution and the same σ is [12]:

$$p_{r_{1}r_{2}}(r_{1}, r_{2}) = \frac{1}{\sqrt{2\pi}\sigma_{1}r_{1}}e^{-\frac{(\ln r_{1}-\mu_{1})^{2}}{2\sigma_{1}^{2}}} \cdot \frac{1}{\sqrt{2\pi}\sigma_{1}\sqrt{1-\rho^{2}r_{2}}}e^{-\frac{\left(\ln r_{2}-\left(\mu_{2}+\rho\frac{\sigma_{2}}{\sigma_{1}}(\ln r_{1}-\mu_{1})\right)\right)^{2}}{2\left(1-\rho^{2}\right)\sigma_{2}^{2}}}$$

(8)

where ρ is correlation coefficient.

The PDF of *r* at the output of SC combiner can be expressed in terms of joint PDF of r_1 and r_2 as [1]:

(9)
$$p_r(r) = \int_0^r p_{r_1, r_2}(r, r_2) dr_2 + \int_0^r p_{r_1, r_2}(r_1, r) dr_2$$

If it is assumed that channels are identical, the distribution parameters for the both branches are the same. Replacing (3-6) in (9), and after some manipulations we obtain PDF of r as:

For
$$r < r_T (r_1 < r_T, r_2 < r_T)$$

 $p_r(r) =$

$$= 2 \frac{1}{\sqrt{2\pi} \sigma r} e^{\frac{(\ln r - \mu)^2}{2\sigma^2}} \left(\frac{1}{2} + erf\left(\frac{\ln r_t - (\mu + \rho(\ln r - \mu))}{\sigma \sqrt{1 - \rho^2} \sqrt{2}} \right) \right) \cdot \int_{0}^{r} \frac{1}{\sqrt{2\pi} \sigma r_1} e^{\frac{(\ln r_t - \mu)^2}{2\sigma^2}} \left(\frac{1}{2} + erf\left(\frac{\ln r_t - (\mu + \rho(\ln r_1 - \mu))}{\sigma \sqrt{1 - \rho^2} \sqrt{2}} \right) \right) dr_1$$

(10)

where erf(x) is error function defined by [13]

(11)
$$erf(x) = \frac{2}{\sqrt{\pi}} \int_{0}^{x} e^{-t^{2}} dt$$

For $r_1 \ge r_T$ ($r_1 \ge r_T$, $r_2 < r_T$)

$$p_{r_{1}}(r) = \int_{0}^{r_{1}} p_{r_{1},r_{2}}(r,r_{2})dr_{2} + \int_{r_{t}}^{r} p_{r_{1},r_{2}}(r_{1},r)dr_{1}$$
(12)
$$p_{r_{1}}(r) = \frac{1}{2\sqrt{2\pi}\sigma r}e^{-\frac{(\ln r-\mu)^{2}}{2\sigma^{2}}}\left(\frac{1}{2} + \frac{1}{2}erf\left(\frac{\ln r-\mu}{\sigma\sqrt{2}}\right)\right).$$

$$\cdot \left(\frac{1}{2} + erf\left(\frac{\ln r_{t} - (\mu + \rho(\ln r - \mu))}{\sigma\sqrt{1 - \rho^{2}}\sqrt{2}}\right)\right) + \frac{1}{\sigma\sqrt{1 - \rho^{2}}\sqrt{2}}.$$

$$\cdot \int_{0}^{r} \frac{1}{\sqrt{2\pi}\sigma r_{1}}e^{-\frac{(\ln r-\mu)^{2}}{2\sigma^{2}}}\left(\frac{1}{2} + erf\left(\frac{\ln r_{t} - (\mu + \rho(\ln r_{1} - \mu))}{\sigma\sqrt{1 - \rho^{2}}\sqrt{2}}\right)\right)dr_{1} + \frac{1}{\sqrt{2\pi}\sigma r}e^{-\frac{(\ln r-\mu)^{2}}{2\sigma^{2}}}\left(\frac{1}{2} + erf\left(\frac{\ln r_{t} - (\mu + \rho(\ln r - \mu))}{\sigma\sqrt{1 - \rho^{2}}\sqrt{2}}\right)\right).$$

$$\cdot \int_{0}^{r} \frac{1}{\sqrt{2\pi}\sigma r_{1}}e^{-\frac{(\ln r_{1} - \mu)^{2}}{2\sigma^{2}}}\left(\frac{1}{2} + erf\left(\frac{\ln r_{t} - (\mu + \rho(\ln r - \mu))}{\sigma\sqrt{1 - \rho^{2}}\sqrt{2}}\right)\right)dr_{1}$$
(13)

For $r_1 \ge r_T$ ($r_1 < r_T$, $r_2 \ge r_T$)

$$p_{r_2}(r) = \int_{r_1}^{r} p_{r_1, r_2}(r, r_2) dr_2 + \int_{0}^{r_1} p_{r_1, r_2}(r_1, r) dr_1$$
(14)

$$p_{r_{2}}(r) = \frac{1}{2\pi\sigma^{2}\sqrt{1-\rho^{2}r}} \left(\frac{1}{2} + erf\left(\frac{\ln r_{t}-\mu}{\sigma\sqrt{2}}\right)\right).$$
$$\cdot \int_{0}^{r} \frac{1}{r_{1}} e^{-\frac{1}{2(1-\rho^{2})} \left[\left(\frac{\ln r-\mu}{\sigma}\right)^{2} + \left(\frac{\ln r_{1}-\mu}{\sigma}\right)^{2} - 2\rho\left(\frac{\ln r-\mu}{\sigma}\right)\left(\frac{\ln r_{1}-\mu}{\sigma}\right)\right]} dr_{1} + \frac{1}{2} \left[\frac{1}{r_{1}} + \frac{1}{r_{1}}\right] dr_{1} + \frac{1}{r_{1}} \left[\frac{1}{r_{1}} + \frac{1}{r_{1}} + \frac{1$$

$$+\frac{1}{\sqrt{2\pi}\sigma r}e^{\frac{-(\ln r-\mu)^{2}}{2\sigma^{2}}}\left(\frac{1}{2}+erf\left(\frac{\ln r_{t}-(\mu+\rho(\ln r-\mu))}{\sigma\sqrt{1-\rho^{2}}\sqrt{2}}\right)\right).$$
$$\cdot\int_{0}^{r}\frac{1}{\sqrt{2\pi}\sigma r_{1}}e^{\frac{-(\ln r_{t}-\mu)^{2}}{2\sigma^{2}}}\left(\frac{1}{2}+erf\left(\frac{\ln r_{t}-(\mu+\rho(\ln r_{1}-\mu))}{\sigma\sqrt{1-\rho^{2}}\sqrt{2}}\right)\right)dr_{1}$$

(15)

For
$$r_{1} \ge r_{T}$$
 $(r_{1} \ge r_{T}, r_{2} \ge r_{T})$
 $p_{r_{3}}(r) = \int_{r_{1}}^{r} p_{r_{1},r_{2}}(r,r_{2})dr_{2} + \int_{r_{1}}^{r} p_{r_{1},r_{2}}(r_{1},r)dr_{1}$
(16)
 $p_{r_{3}}(r) =$
 $= \frac{2}{2\pi\sigma_{2}^{2}\sqrt{1-\rho^{2}}r} \cdot \cdot \int_{r_{1}}^{r} \frac{1}{r_{1}}e^{-\frac{1}{2(1-\rho^{2})}\left[\left(\frac{\ln r-\mu}{\sigma}\right)^{2} + \left(\frac{\ln r_{1}-\mu}{\sigma}\right)^{2} - 2\rho\left(\frac{\ln r-\mu}{\sigma}\right)\left(\frac{\ln r_{1}-\mu}{\sigma}\right)\right]}dr_{1} + \frac{1}{r_{1}}e^{-\frac{1}{2(1-\rho^{2})}\left[\left(\frac{\ln r-\mu}{\sigma}\right)^{2} + \left(\frac{\ln r_{1}-\mu}{\sigma}\right)^{2} - 2\rho\left(\frac{\ln r-\mu}{\sigma}\right)\left(\frac{\ln r_{1}-\mu}{\sigma}\right)\right]}dr_{1} + \frac{1}{r_{1}}e^{-\frac{1}{2(1-\rho^{2})}\left[\left(\frac{\ln r-\mu}{\sigma}\right)^{2} + \left(\frac{\ln r_{1}-\mu}{\sigma}\right)^{2} - 2\rho\left(\frac{\ln r-\mu}{\sigma}\right)\left(\frac{\ln r_{1}-\mu}{\sigma}\right)\right]}dr_{1} + \frac{1}{r_{1}}e^{-\frac{1}{2(1-\rho^{2})}\left[\left(\frac{\ln r-\mu}{\sigma}\right)^{2} + \left(\frac{\ln r_{1}-\mu}{\sigma}\right)^{2} - 2\rho\left(\frac{\ln r-\mu}{\sigma}\right)\left(\frac{\ln r_{1}-\mu}{\sigma}\right)\right]}dr_{1} + \frac{1}{r_{1}}e^{-\frac{1}{2(1-\rho^{2})}\left[\left(\frac{\ln r-\mu}{\sigma}\right)^{2} + \left(\frac{\ln r_{1}-\mu}{\sigma}\right)^{2} - 2\rho\left(\frac{\ln r-\mu}{\sigma}\right)\left(\frac{\ln r_{1}-\mu}{\sigma}\right)\right]}dr_{1} + \frac{1}{r_{1}}e^{-\frac{1}{2(1-\rho^{2})}\left[\left(\frac{\ln r-\mu}{\sigma}\right)^{2} + \left(\frac{\ln r_{1}-\mu}{\sigma}\right)^{2} - 2\rho\left(\frac{\ln r}{\sigma}\right)\left(\frac{\ln r_{1}-\mu}{\sigma}\right)\right]}dr_{1} + \frac{1}{r_{1}}e^{-\frac{1}{2(1-\rho^{2})}\left[\left(\frac{\ln r}{\sigma}\right)^{2} + \left(\frac{\ln r}{\sigma}\right)^{2} + \left(\frac{\ln r}{\sigma}\right)^{2} - 2\rho\left(\frac{\ln r}{\sigma}\right)\left(\frac{\ln r}{\sigma}\right)\left(\frac{\ln r}{\sigma}\right)\right]}dr_{1} + \frac{1}{r_{1}}e^{-\frac{1}{2(1-\rho^{2})}\left[\left(\frac{\ln r}{\sigma}\right)^{2} + \left(\frac{\ln r}{\sigma}\right)^{2} + \left(\frac{\ln r}{\sigma}\right)^{2} + \left(\frac{\ln r}{\sigma}\right)\left(\frac{\ln r}{\sigma}\right)\left(\frac{\ln r}{\sigma}\right)\right]}dr_{1} + \frac{1}{r_{1}}e^{-\frac{1}{2(1-\rho^{2})}\left[\left(\frac{\ln r}{\sigma}\right)^{2} + \left(\frac{\ln r}{\sigma}\right)\left(\frac{\ln r}{\sigma}\right)^{2} + \left(\frac{\ln r}{\sigma}\right)\left(\frac{\ln r}{\sigma}\right)\left(\frac{\ln r}{\sigma}\right)\right]}dr_{1} + \frac{1}{r_{1}}e^{-\frac{1}{2(1-\rho^{2})}\left[\left(\frac{\ln r}{\sigma}\right)^{2} + \left(\frac{\ln r}{\sigma}\right)\left(\frac{\ln r}{\sigma}\right)\left(\frac{\ln r}{\sigma}\right)\right]}dr_{1} + \frac{1}{r_{1}}e^{-\frac{1}{2(1-\rho^{2})}\left[\left(\frac{\ln r}{\sigma}\right)\left(\frac{\ln r}{\sigma}\right)\left(\frac{\ln r}{\sigma}\right)\left(\frac{\ln r}{\sigma}\right)\right]}dr_{1} + \frac{1}{r_{1}}e^{-\frac{1}{2(1-\rho^{2})}\left[\left(\frac{\ln r}{\sigma}\right)\left(\frac{\ln r}{\sigma}\right)\left(\frac{\ln r}{\sigma}\right)\left(\frac{\ln r}{\sigma}\right)\right]}dr_{1} + \frac{1}{r_{1}}e^{-\frac{1}{2(1-\rho^{2})}\left[\left(\frac{\ln r}{\sigma}\right)\left(\frac{\ln r}{\sigma}\right)\left(\frac{$

$$+ 2 \frac{1}{2\pi\sigma^{2}\sqrt{1-\rho^{2}r}} \left(\frac{1}{2} + erf\left(\frac{\ln r_{t}-\mu}{\sigma\sqrt{2}}\right)\right) \cdot \frac{1}{2\pi\sigma^{2}\sqrt{1-\rho^{2}r}} \left[\frac{\ln r-\mu}{\sigma}\right]^{2} + \left(\frac{\ln r_{t}-\mu}{\sigma}\right)^{2} - 2\rho\left(\frac{\ln r-\mu}{\sigma}\right)\left(\frac{\ln r_{t}-\mu}{\sigma}\right)\right] dr_{1} + \frac{1}{\sqrt{2\pi\sigma}r} e^{-\frac{(\ln r-\mu)^{2}}{2\sigma^{2}}} \left(\frac{1}{2} + \frac{1}{2}erf\left(\frac{\ln r-\mu}{\sigma\sqrt{2}}\right)\right) \cdot \left(\frac{1}{2} + erf\left(\frac{\ln r_{t}-(\mu+\rho(\ln r-\mu))}{\sigma\sqrt{1-\rho^{2}}\sqrt{2}}\right)\right) + \frac{1}{\sqrt{2\pi\sigma}r} e^{-\frac{(\ln r-\mu)^{2}}{2\sigma^{2}}} \cdot \frac{1}{2} + erf\left(\frac{\ln r_{t}-(\mu+\rho(\ln r_{1}-\mu))}{\sigma\sqrt{1-\rho^{2}}\sqrt{2}}\right)\right) dr_{1} + 2\frac{1}{\sqrt{2\pi\sigma}r} e^{-\frac{(\ln r-\mu)^{2}}{2\sigma^{2}}} \left(\frac{1}{2} + erf\left(\frac{\ln r_{t}-(\mu+\rho(\ln r_{1}-\mu))}{\sigma\sqrt{1-\rho^{2}}\sqrt{2}}\right)\right) dr_{1} + 2\frac{1}{\sqrt{2\pi\sigma}r} e^{-\frac{(\ln r-\mu)^{2}}{2\sigma^{2}}} \left(\frac{1}{2} + erf\left(\frac{\ln r_{t}-(\mu+\rho(\ln r-\mu))}{\sigma\sqrt{1-\rho^{2}}\sqrt{2}}\right)\right) dr_{1} + \frac{1}{2\pi\sigma}r e^{-\frac{(\ln r-\mu)^{2}}{2\sigma^{2}}} \left(\frac{1}{2} + erf\left(\frac{\ln r_{t}-(\mu+\rho(\ln r-\mu))}{\sigma\sqrt{1-\rho^{2}}\sqrt{2}}\right)\right) dr_{1} + \frac{1}{2\pi\sigma}r e^{-\frac{(\ln r-\mu)^{2}}{2\sigma^{2}}} \left(\frac{1}{2} + erf\left(\frac{\ln r_{t}-(\mu+\rho(\ln r-\mu))}{\sigma\sqrt{1-\rho^{2}}\sqrt{2}}\right)\right) dr_{1} + \frac{1}{2\pi\sigma}r e^{-\frac{(\ln r_{t}-\mu)^{2}}{2\sigma^{2}}} \left(\frac{1}{2} + erf\left(\frac{\ln r_{t}-(\mu+\rho(\ln r_{t}-\mu))}{\sigma\sqrt{1-\rho^{2}}\sqrt{2}}\right)\right) dr_{1} + \frac{1}{2\pi\sigma}r e^{-\frac{(\ln r_{t}-\mu)^{2}}{2\sigma^{2}}} \left(\frac{1}{2} + erf\left(\frac{\ln r_{t}-(\mu+\rho(\ln r_{t}-\mu))}{\sigma\sqrt{1-\rho^{2}}\sqrt{2}}\right)\right) dr_{1} + \frac{1}{2\pi\sigma}r e^{-\frac{(\ln r_{t}-\mu)^{2}}{2\sigma^{2}}} \left(\frac{1}{2} + erf\left(\frac{\ln r_{t}-(\mu+\rho(\ln r_{t}-\mu))}{\sigma\sqrt{1-\rho^{2}}\sqrt{2}}\right)\right) dr_{1} + \frac{1}{2\pi\sigma}r e^{-\frac{(\ln r_{t}-\mu)^{2}}{2\sigma^{2}}} \left(\frac{1}{2} + erf\left(\frac{\ln r_{t}-(\mu+\rho(\ln r_{t}-\mu))}{\sigma\sqrt{1-\rho^{2}}\sqrt{2}}\right)\right) dr_{1} + \frac{1}{2\pi\sigma}r e^{-\frac{(\ln r_{t}-\mu)^{2}}{2\sigma^{2}}} \left(\frac{1}{2} + erf\left(\frac{\ln r_{t}-\mu}{\sigma\sqrt{1-\rho^{2}}\sqrt{2}}\right) dr_{1} + \frac{1}{2\pi\sigma}r e^{-\frac{(\ln r_{t}-\mu)^{2}}{2\sigma^{2}}} dr_{1} + \frac{1}{2\pi\sigma}r e^{-\frac{(\ln r_{t}-\mu)^{2}}{2\sigma^{2}} dr_{1} + \frac{1}{2\pi\sigma}r e^{-\frac{(\ln r_{t}-\mu)^{2}}{2\sigma^{2}}} dr_{1} + \frac{1}{2\pi\sigma}r e^{-\frac{(\ln r_{t}-\mu)^{2}}{2\sigma^$$

Overall pdf for $r_1 \ge r_T$ ($r_1 \ge r_T$, $r_2 < r_T$; $r_1 < r_T$, $r_2 \ge r_T$; $r_1 \ge r_T$, $r_2 \ge r_T$; $r_1 \ge r_T$, $r_2 \ge r_T$) is

(18)
$$p_r(r) = p_{r_1}(r) + p_{r_2}(r) + p_{r_3}(r)$$

The PDF is obtained in the form of one dimension integral with finite bounds.

The outage probability is very useful performance measure for diversity systems operating in fading environments defined as the probability that output SIR of the SC falls below a given threshold r also known as a protection ratio. The outage probability $P_{out}(r)$ is defined as: (19) $P_{-}(r) = P(r_1 \le r, r_2 \le r)$

(13)
$$I_{out}(r) - I(r_1 \le r, r_2 \le r_3)$$

For
$$r < r_T (r_1 < r_T, r_2 < r_T)$$

(20)
$$P_{out}(r) = \int_{0}^{r} p_r(r) dr$$

For
$$r_1 \ge r_T$$
 $(r_1 \ge r_T, r_2 < r_T; r_1 \ge r_T, r_2 \ge r_T; r_1 \ge r_T, r_2 \ge r_T)$

(21)
$$P_{out}(r) = \int_{0}^{r_t} p_r(r) dr + \int_{r_t}^{r} p_r(r) dr$$

The Numerical Results

We present some values of the outage probabilities for different types of combiners and correlation parameters in Figures 2 and 3. The optimum thresholds $r_T = exp(\mu + \sigma^2/2)$ are adopted for SSC combiners [1].

In Fig. 2. we show the family of curves for the outage probabilities for one channel receiver and for SSC and SC combiners at one time instant and SSC/SC combiner at two time instants for uncorrelated case and for very strong correlation. We can see that SSC/SC combiner has significant better performances for uncorrelated case and for ρ =1 the CDF of SSC/SC combiner for $r < r_T$ follows the results for SC combiner at one time instant and for SSC combiner otherwise.



Fig.2. Outage probability for different types of combiners for parameters $\mu = l$, $\sigma = 0.5$, $\rho = 0; l$



Fig.3. Outage probability at the output of SSC/SC combiners for parameters μ =1, σ =0.5 for different values of ρ

Observing the characteristics of SSC/SC combiner at two time instants from Figure 3. it is obvious that benefits of the use of this kind of combiner increases with decreasing of correlation between input signals, and therefore results in better system performances.

Conclusion

The probability density function of dual SSC/SC combiner output signal at two time instants in the presence of lognormal fading is determined. The system performances deciding by two samples can be determine by the joint probability density function of the SSC combiner output signal at two time instants and putting them as inputs of SC combiner. Then, the outage probability is numerically calculated using this PDF.

The obtained results are shown graphically to compare performances of the SSC/SC combiner with regard to classical SSC and SC combiners at one time instant. We emphasize improving of the SSC/SC combiner characteristics at two time instants comparing with classical SSC and SC combiners at one time instant. It can be seen that this is not valid only for the very strong correlation between inputs, where there is not a gain of using this type of complex combiner

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