

Optimal Placement of Traveling Wave Fault Location Equipment in Power Grid Based on Characteristic Non-singular Set

Abstract. With the widely use of traveling wave fault location equipment (TWFL) in power grid, network-based traveling wave fault location (NBTWFL) method has been proposed. To ensure the effectiveness and economy of NBTWFL method, based on the principle of characteristic non-singular set, an optimal placement algorithm of TWFL is proposed in this paper. The corresponding NBTWFL method based on maximum non-singular subset, additional installation plan of TWFL and some other related problems are also discussed in this paper.

Streszczenie. W artykule opisano metodę wykrywania awarii w sieci elektroenergetycznej na podstawie analizy fali wędrującej. Proponowane rozwiązanie bazuje na klasycznym algorytmie wykrywania fali wędrującej, w którym zastosowano niesingularne wartości własne. Pozwoliło to na optymalizację rozmieszczenia urządzeń do wykrywania awarii. (Optymalizacja rozmieszczenia czujników wykrywania fali wędrującej przy awarii w sieci elektroenergetycznej na podstawie niesingularnego ułożenia wartości własnych).

Keywords: Optimal placement, Traveling wave, Fault location, non-singular set.

Słowa kluczowe: optymalne rozmieszczenie, fala wędrująca, lokalizacja awarii, niesingularne rozmieszczenie.

1 Introduction

Since the 90's in 20th century, rapid development of modern microelectronics, global position system (GPS), communications and digital signal processing (DSP) technology provides the foundation for research and development of traveling wave fault location equipment (TWFL). As the major breakthroughs in extraction technology of transient traveling [1-3], the principle and algorithm of traveling wave fault location [4-12] and etc., TWFL has been widely applied into the power grid.

For traditional both-terminal traveling wave fault location method (BTTWFL) based on single transmission line, any fault in TWFL like start-up failure and time record error will result in location failure. Field data of B.C Hydro power grid showed that traveling wave could propagate over thousands of kilometres and every substation could detect the fault-generated traveling wave [1]. Meanwhile, theory and practice have proved that speed of aerial-mode traveling wave can basically maintain invariable in a certain range [13]. So the literature [14-16] proposed a network-based traveling wave fault location method (NBTWFL), in which the fault position is located based on all the arrival time of initial wave-fronts of traveling wave recorded by the TWFL installed at every substation of the power grid.

Compared to the BTTWFL method, NBTWFL method can provide more reliable and accurate location result. However, at present TWFL is too expensive and modern power grid is too large, it's uneconomical and unnecessary to install TWFL at every substation. Thus literature [17] proposed the principle of optimal placement of TWFL in power grid. The method proposed in the paper [17] has a certain value which used simulated annealing algorithm to confirm optimal placement plan, but it needs to be verified by NBTWFL algorithm in the progress. Directly based on NBTWFL algorithm, literature [18] firstly assumed that each transmission line was the fault line, and then optimal placement plan could be obtained from the minimum sharing set which was determined through the substations located at both sides of the fault line. Besides, literature [19] proposed an optimal placement algorithm of TWFL based on multi-DOF (Degree of Freedom). To obtain the multi-DOF, the principle of maximum non-singular subset is presented. But the algorithm needs to be improved to adapt to ring configuration.

Actually NBTWFL method is the extension of traditional BTTWFL method, based on this principle, a new optimal placement algorithm of TWFL based on characteristic

non-singular set is presented in this paper. It proposed a clear physical conception and can be achieved easily.

2 Basic principle

2.1 Extension of traditional BTTWFL method

The principle of traditional BTTWFL method is to use the arrival time difference of the initial wave-fronts of traveling wave recorded by the TWFL at both sides of the fault line. As shown in Fig. 1(a), a fault happened at point F on line BC, the recorded arrival time of transient traveling wave at substation A,B,C,D and E is T_A, T_B, T_C, T_D, T_E , respectively. Then the basic calculation equation of BTTWFL method is as follows:

$$(1) X_{BF} = \frac{1}{2}[(T_B - T_C)v + L_{BC}]$$

where: v – the velocity of traveling wave, L_{BC} – the length of line BC.

Because of the transmission, traveling wave can propagate through substation B to A and propagate through C to D and E. Regard the path A-B-C-D-E as an equivalent extended line, then fault position can be located by the following equation:

$$(2) X_{AF} = \frac{1}{2}[(T_A - T_E)v + L_{AE}]$$

Equation (2) is the basic calculation formula of NBTWFL method. The basic principle of NBTWFL method is to decompose the whole power grid into several extended lines. The extended line is relative to the basic line like line BC.

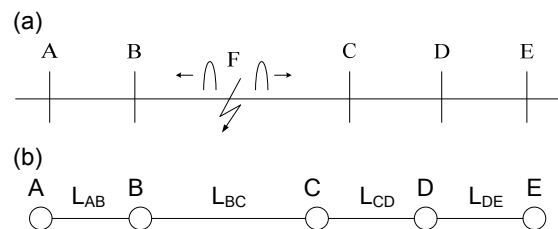


Fig.1. Extension of traditional both-terminal traveling wave fault location method

2.2 Some basic definition

In graph theory, when characteristics of power elements are ignored and only propagation path of the initial wave-fronts is taken into consideration, the power grid can be abstracted as a topological graph $G=(V, E)$ which is

constructed by n vertexes and b edges. In graph G , V represented the set of vertexes and E represented the set of edges. Vertexes and edges are corresponding to substations and transmission lines, respectively. The weight of edge e_i represents the length of the corresponding transmission line [20]. The topological graph of the power grid shown in Fig. 1(a) is given in Fig. 1(b).

The adjacency matrix of the simple graph $G=(V,E)$ which is represented by $A(G)=(a_{ij})_{n \times n}$ can be defined as follows:

$$(3) \quad a_{ij} = \begin{cases} 1, & i \neq j \& (v_i, v_j) \in E \\ 0, & \text{otherwise} \end{cases}$$

The weight matrix of the simple graph $G=(V,E)$ which is represented by $W(G)=(\omega_{ij})_{n \times n}$ can be defined as follows:

$$(4) \quad \omega_{ij} = \begin{cases} 0, & i = j \\ f(v_i, v_j), & (v_i, v_j) \in E \\ \infty, & \text{otherwise} \end{cases}$$

where: $f(v_i, v_j)$ - the weight of the edge v_i, v_j .

In graph $G=(V,E)$, the degree of vertex v_i which is represented by $d(v_i)$ is defined as the number of edges related to v_i :

$$(5) \quad d(v_i) = \sum_{j=1}^n a_{ij}$$

In graph $G=(V, E)$, assuming P_{uv} represents the minimum path between vertex u and v , P_{rs} represents the minimum path between vertex r and s . If path P_{rs} completely contains P_{uv} , then it is represented by $P_{uv} \subset P_{rs}$. Otherwise they would be regarded as totally different paths and the relationship is represented by $P_{uv} \cap P_{rs} = \Phi$.

The set of minimum path between vertex u and the other vertexes is identified as the minimum path tree of vertex u , represented by $Tree_u$. $Ctree_u$ is the maximum non-singular subset of $Tree_u$ if it meets the following conditions: (1) for any two elements P_{uv} and P_{rs} ($P_{uv} \in Ctree_u$, $P_{rs} \in Ctree_u$), $P_{uv} \cap P_{rs} = \Phi$; (2) for any elements P_{uw} ($P_{uw} \in Tree_u$), if there is no P_{ui} ($P_{ui} \in Tree_u$) can meet $P_{uw} \subset P_{ui}$, then $P_{uw} \in Ctree_u$.

2.3 Basic principle of optimal placement of TWFL

In the simple power grid shown in Fig. 1(a), according to equation (2), the progress of optimal placement of TWFL can be defined as follows: (1) find out the maximum extensive line P_{rs} which contains the fault line BC (for any extensive line P_{uv} , it meets: if $P_{uv} \supset P_{BC}$, then $P_{uv} \subset P_{rs}$); (2) confirm the optimal placement plan which is that two TWFL are installed at the both terminals of the maximum extensive line P_{rs} .

3 Optimal placement of TWFL

3.1 Principle of optimal placement of TWFL

According to the above analysis, the key of optimal placement of TWFL is how to find out the maximum extensive line. In this paper, it is solved by use of graph theory.

In graph theory, maximum extensive line of vertex u is just the path between the root node and the leaf node in the minimum path tree of u which can be obtained by Dijkstra algorithm [20-22]. Because fault may happen at every basic line, the maximum extensive line set is just the maximum non-singular subset of the maximum non-singular subset of all vertexes, and it is called the maximum non-singular set of the graph in this paper. For the simple power grid shown in Fig. 1(a), the maximum non-singular set of the graph is $\{A-B-C-D-E\}$.

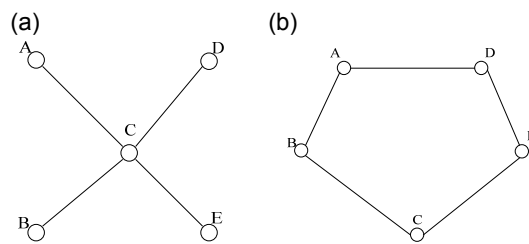


Fig. 2. Star and ring configurations

Besides of linear configuration shown in Fig. 1(a), star and ring configurations also exist in power grid which is shown in Fig. 2. Dimensionality of maximum non-singular set in star or ring configuration is more than 1, so principle of characteristic non-singular set of the edge is proposed to solve the problem of confirming optimal placement plan based on several maximum extensive lines. Set $Ctree_G$ as the maximum non-singular set of graph $G=(V, E)$ and assuming that $P_{rs} \in Ctree_G$, $P_{uv} \in Ctree_G$ and b is one edge of G . Then $Ctree_b$ is the characteristic non-singular set of b if it meets the following conditions: (1) if $b \subset P_{rs}$, $P_{rs} \in Ctree_b$; (2) any $P_{uv} \notin Ctree_b$, $b \not\subset P_{uv}$.

In addition, the following principle is used in optimal placement of TWFL:

(1) TWFL must be installed at the vertex whose degree equals 1, in this paper it is called must-be-installed vertex (MBIV).

(2) TWFL is unnecessary to be installed at the vertex which is related to MBIV and its degree is more than 1. In this paper it is called unnecessary-be-installed vertex (UBIV).

The MBIV and UBIV can be identified based on equation (5): vertex i would be MBIV if the following condition is met: $\sum a_{ij}=1 (1 \leq j \leq n)$; vertex i would be UBIV if the following condition is met: $\sum a_{ij} > 1 (1 \leq j \leq n)$ and there exists at least one element which meets $a_{ip}=1$ (p is MBIV).

3.2 Optimal placement of TWFL

The optimal placement algorithm of TWFL can be derived as follows:

(1) Based on the structure of the power grid, obtain the corresponding topological graph, adjacency matrix and weight matrix.

(2) Identify the MBIV and UBIV.

(3) Figure out the maximum non-singular subsets of all vertexes except for the UBIV by use of Dijkstra algorithm.

(4) Obtain the maximum non-singular set of the graph and the corresponding characteristic non-singular set of each edge. Smaller dimensionality of the characteristic non-singular set is according to the smaller number of maximum extensive lines which contain the basic line, so TWFL would be more necessary to be installed at the endpoints of the elements belonging to the characteristic non-singular set whose dimensionality is smaller.

(5) In ascending order, sort edges by the dimensionality of the corresponding characteristic non-singular set. When the breaker status is unknown, the corresponding edge will not be taken into consideration in the next progress if there exists at least one element of its characteristic non-singular set on which two TWFL have been installed and they are on both sides of the edge; when the breaker status is a known quantity, the corresponding edge will not be taken into consideration in the next progress if two TWFL have been installed at the nodes of the elements which belongs to characteristic non-singular set of the edge, and they can't be located at the same side of the edge in the traveling wave propagation path.

(6) Select the characteristic non-singular set whose dimensionality is the minimum as the TWFLF-prior-installation unit. If the breaker status is unknown, two TWFLF should be installed at the both endpoints of one element and the element whose one endpoint has installed TWFLF takes priority of selection. If the breaker status is a known quantity, Two TWFLF should be installed at any two endpoints of elements but need to be on both sides of the corresponding edge.

(7) Repeat step (5) and (6) until there exists no edge to be sorted.

From step (6), it can be inferred that the optimal placement plan may not be unique if the number of characteristic non-singular sets which has the minimum dimensionality is more than 1 or the alternative nodes which need to install TWFLF are not unique.

4 Case study

As shown in Fig. 3, take the 500kV power grid in Hunan Province of China mentioned in literature [14] as an example, the progress of confirming optimal placement plan is as follows:

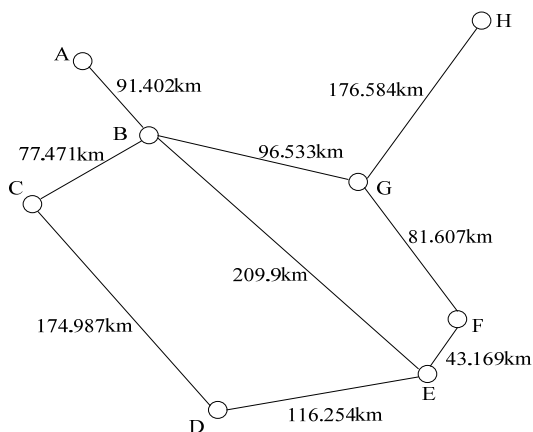


Fig. 3. 500kV power grid in Hunan province, China

(1) Obtain the corresponding adjacency matrix $A(G)$ and weight matrix $W(G)$.

(2) The MBIV is vertex A and H; the UBIV is B and G.

(3) Maximum non-singular subsets of all vertexes except for the UBIV are shown in Table 1.

(4) The maximum non-singular set of the graph and the corresponding characteristic non-singular set of each edge are shown in Table 2.

(5) If the breaker status is unknown, the iterative progress of the optimal placement is shown in Table 3. If the breaker status is known, similar iterative progress is used to get the optimal placement plan.

Results show that the optimal placement plan with the breaker status in 500kV power grid in Hunan Province of China is the same as the optimal placement plan without the breaker status. It is as follows: Four TWLFE should be installed at substation A, H, D and E separately. The effectiveness of the optimal placement algorithm mentioned above is obvious, it can meet the requirements of reliability and economy. When a fault happened on any transmission line, at least one element of maximum non-singular set of the graph on which TWFLF have been installed can be used to locate the fault position; meanwhile, the installation number of TWFLF is the minimum. The optimal placement plan in literature [17] is $P = [A, B, D, E, H]$, obviously it is not optimal. The optimal placement plan obtained in this paper is the same as the result in literature [18], but the algorithm proposed in this paper is simpler, more convenient and supported by adequate evidence. Meanwhile, through

combination of the optimal placement algorithm and the NBTWFL method based on maximum non-singular set mentioned below, the fault position can be located without breaker status.

Table 1. Maximum non-singular subsets of all vertexes except for the UBIV in power grid shown in Fig. 3

Vertex	Maximum non-singular subset	Vertex	Maximum non-singular subset
A	A-B-C-D A-B-E A-B-G-F A-B-G-H	E	E-D E-B-C E-B-A E-F-G-H
B	UBIV	G	UBIV
C	C-B-A C-B-E C-B-G-F C-B-G-H	F	F-E-D F-G-B-C F-G-B-A F-G-H
D	D-C-B-A D-E-F-G-H	H	H-G-B-C H-G-B-A H-G-F-E-D

Table 2. Maximum non-singular set of the graph and the corresponding characteristic non-singular set of each edge in power grid shown in Fig. 3

Maximum non-singular set of graph	Edge	Characteristic non-singular set
A-B-C-D A-B-E A-B-G-F A-B-G-H C-B-E C-B-G-F C-B-G-H D-E-F-G-H	AB	A-B-C-D A-B-E A-B-G-H
	BC	A-B-C-D C-B-E C-B-G-F C-B-G-H
	CD	A-B-C-D
	DE	D-E-F-G-H
	EF	D-E-F-G-H
	BE	A-B-E C-B-E
	FG	A-B-G-F C-B-G-F D-E-F-G-H
	BG	A-B-G-F A-B-G-H C-B-G-F C-B-G-H
	GH	A-B-G-H C-B-G-H D-E-F-G-H

Table 3. The iterative progress of the optimal placement without breaker status in power grid shown in Fig. 3

	The vertexes which install TWFLF	Sort of edges	Number of elements	If or not to be considered in next step
Initial Status	A, H	CD	1	Yes
		DE	1	Yes
		EF	1	Yes
		BE	2	Yes
		AB	3	No
		FG	3	Yes
		GH	3	No
		BC BG	4 4	Yes No
First step	A, H, D	CD	1	No
		DE	1	No
		EF	1	No
		BE	2	Yes
		FG BC	3 4	No No
Second step	A, H, D, E	BE	2	No

(1) D is the substation which traveling wave arrives at first and the corresponding maximum extensive lines which contain the substation D have A-B-C-D and D-E-F-G-H.

(2) The result of fault location is shown in Table 5.

The final result of fault location proved that fault line can be identified correctly and the error of fault location is only -0.116km. The NBTWFL method without breaker status based on the maximum non-singular set can work effectively.

Table 5. The result of fault location without the breaker status

The maximum extensive line	If or not at the substation	Virtual fault location/km	Final result
A-B-C-D	No	$X_{Df} = 29.884$	On line CD and is 29.884km from D
D-E-F-G-H	Yes	$X_{Df} = -0.230$	

5.3 Limitation of NBTWFL method

A. NBTWFL method in ring configuration

When a fault happened at position F shown in Fig. 5(a), the propagation path of initial wave-fronts of traveling wave may change because of the different relative lengths of the edges. Unlike the situations shown in Fig. 5(b) and Fig. 5(c), fault positions in Fig. 5(d) and Fig. 5(e) are not on the extensive line any more, and fault location will fail based on equation (2). So the fault position needs other measures to be located [4-12].

The situations shown in Fig. 5(d) and Fig. 5(e) may happen in the ring configuration when the following conditions are met:

$$(9) \begin{cases} \Delta l < [L_{BC} - (L_{AB} + L_{AC})] / 2 \\ L_{BC} > L_{AB} + L_{AC} \end{cases}$$

where: Δl – the distance between fault position and the terminal of faulty line, L_{BC} – the length of faulty line. L_{AB} & L_{AC} – The length of healthy line.

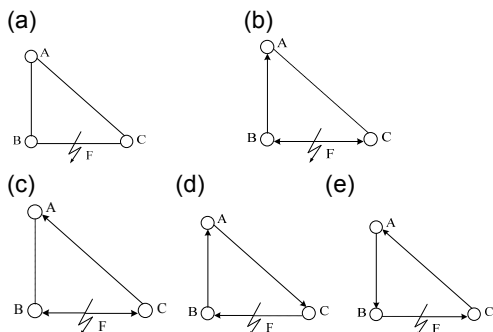


Fig. 5 Different propagation paths in ring configuration

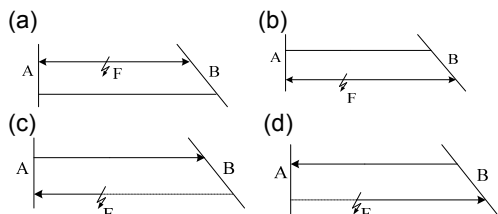


Fig. 6 Different propagation paths in double circuit lines

B. NBTWFL in double circuit lines

If lengths of double circuit lines are the same, the double circuit lines can be equivalent to one line in fault location. However, when lengths of double circuit lines are different, propagation path of initial wave-fronts of transient traveling wave may change because of different fault positions. In Fig. 6(a) or Fig. 6(b), fault position is still on the line AB and it can be located. In Fig. 6(c) and Fig. 6(d), fault positions are not on the line AB any more, and fault location will fail

based on equation (2). So the fault position needs other measures to be located [4-12].

The situation shown in Fig. 6(c) and Fig. 6(d) may happen in the double circuit lines configuration when the following conditions are met:

$$(10) \begin{cases} \Delta l < (L_1 - L_2) / 2 \\ L_1 > L_2 \end{cases}$$

where: Δl – the distance between fault position and the terminal of faulty line, L_1 – the length of the longer line, L_2 – the length of the shorter line.

6 Conclusion

This paper proposed an optimal placement algorithm of TWFL in power grid. It can keep the installation number of TWFL to minimum and locate the fault position on any transmission line. The conclusion of this paper is as follows:

(1) The maximum non-singular set of the topological graph can be obtained by use of Dijkstra algorithm and power grid can be decomposed into several maximum extensive lines based on it. Then optimal placement plan can be confirmed according to this principle.

(2) The optimal placement algorithm based on characteristic non-singular set can work well whether or not breaker status is known.

(3) The optimal placement algorithm based on characteristic non-singular set can be completely combined with the NBTWFL method based on maximum non-singular set in principle. This not only can simplify the calculation procedure and inherently eliminate the virtual fault positions, but also can locate the fault position correctly without breaker status.

(4) The proposed optimal placement algorithm of TWFL can be achieved easily and satisfy the requirement of power grid's operation.

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REFERENCES

- [1] Lee H, Mousa A M, GPS traveling wave fault locator system: investigation into the anomalous measurements related to lightning strikes, *IEEE Trans. On Power Delivery*, 11(1996), No.3, 1214-1223.
- [2] Xinzhou D, Yaozhong G, Bingyin X, Research of fault location based on current traveling waves, *Proceedings of the CSEE*, 19(1999), No. 4, 76-80.
- [3] Xiangjun Z, Xianggen Y, Fuchang L, et al, Study on fault location for transmission lines based on the sensor of traveling-wave, *Proceedings of the CSEE*, 22(2002), No. 6, 42-46.
- [4] Sioziny, V, Transmission line fault distance measurement based on time difference between traveling wave reflection and refraction, *ELEKTRONIKA IR ELEKTROTECHNIKA*, 98(2010), No.2, 25-28.
- [5] Bernadic A, Leonowicz Z, Power line fault location using the Complex Space-Phasor and Hilbert-Huang Transform, *PRZEGLAD ELEKTROTECHNICZNY*, 87(2011), No. 5, 204-207.
- [6] Liu YD, Sheng GH, He ZM, et al, A traveling wave fault location method for earth faults based on mode propagation time delays of multi-measuring points, *PRZEGLAD ELEKTROTECHNICZNY*, 88(2012), No. 3A, 254-258.
- [7] Tayebi SM, Kazemi A, Rezaeipour R, A fault direction discrimination scheme based on transients generated by faults in multi-branch power systems, *International Review of Electrical Engineering*, 7(2012), No. 1, 3586-3591.
- [8] Lin XN, Zhao F, Wu G, et al, Universal wavefront positioning correction method on traveling-wave-based fault-location algorithms, *IEEE Tans. On Power Delivery*, 27(2012), No. 3, 1601-1610.
- [9] Huang Q, Zhen W, Pong PWT, A novel approach for fault location of overhead transmission line with noncontact

- magnetic-field measurement, *IEEE Trans. On Power Delivery*, 27(2012), No. 3, 1186-1195.
- [10] Lin S, He ZY, Li XP, et al, Traveling wave time-frequency characteristic-based fault location method for transmission lines, *IET Generation Transmission & Distribution*, 6(2012), No. 8, 764-772.
- [11] Tabatabaei A, Mosavi MR, Rahmati A, Fault location techniques in power system based on traveling wave using wavelet analysis and GPS timing, *PRZEGLAD ELEKTRO-TECHNICZNY*, 88(2012), No. 6, 347-350.
- [12] Mardiana R, Al Motairy H, Su CQ, Ground fault location on a transmission line using high-frequency transient voltages, *IEEE Trans. On Power Delivery*, 26(2011), No. 2, 1298-1299.
- [13] Jian Q, Xiangxun C, Jianchao Zheng, Study on dispersion of traveling wave in transmission line, *Proceedings of the CSEE*, 19(1999), No. 9, 27-31.
- [14] Xiangjun Z, Nan C, Zewen L, et al, Network-based algorithm for fault location with traveling wave, *Proceedings of the CSEE*, 28(2008), No. 31, 48-53.
- [15] Lin D, Hongye C, Weigen C, et al, Network path based algorithm for regional power grid fault locating with traveling wave, *Automation of Electric Power Systems*, 34(2010), No. 24, 60-64.
- [16] Zewen L, Jiangang Y, Xiangjun Z, et al, Power grid fault traveling wave network protection scheme, *International Journal of Electrical Power and Energy Systems*, 33(2011), No. 4, 875-879.
- [17] Zewen L, Jiangang Y, Xiangjun Z, et al, Optimal placement of traveling wave fault location equipment for power grid, *Automation of Electric Power Systems*, 33(2009), No. 3, 64-68.
- [18] Feng D, Nan C, Xiangjun Z, et al, An optimal configuration algorithm for traveling wave fault location equipments in power grid based on graph theory, *Automation of Electric Power Systems*, 34(2010), No. 11, 87-92.
- [19] Xuyong H, Wenhui Z, Pei L, Optimal placement of traveling wave fault locating equipment and its improved algorithm, *Electric Power Automation Equipment*, 30(2010), No. 1, 41-44.
- [20] Douglas B. West, Introduction to graph theory, 3rd edition, published by Prentice Hall, 2007.
- [21] Gunkel C, Stepper A, Muller AC, et al, Micro crack detection with Dijkstra's shortest path algorithm, *Machine Vision And Applications*, 23(2012), No. 3, 589-601.
- [22] Hofner P, Moller B, Dijkstra, Floyd and Warshall meet Kleene, *Formal Aspects Of Computing*, 24(2012), No. 4-6, 459-476.
- [23] Zumberge JF, Heflin MB, Jefferson DC, et al, Precise point positioning for the efficient and robust analysis of GPS data from large networks, *Journal of Geophysical Research-solid Earth*, 102(1997), No. B3, 5005-5017.

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