Anticollision manoeuvre optimization in the NAVDEC system

Abstract. Authors presented the concept of improved time optimization algorithm of anticollision manoeuvre to be implemented in the NAVDEC system. The algorithm will play an important role in supporting the navigator in decision making process. Moreover implementation of the algorithm will reduce significantly fuel consumption. In conclusion, safety and economic efficiency of shipping will be improved.

Słowa kluczowe: decision support, anticollision, optimization, NAVDEC.

Introduction

Supporting the navigator in making decisions may significantly enhance the safety and effectiveness of the transport process. The navigational decision support system is to supplement the shipborne navigational equipment, while in the future it may be a part of Integrated Bridge System (IBS). The correct operation of the system requires co-operation with other devices and systems on board ship and the external ones in order to acquire navigational information automatically. Apart from the presentation of navigational situation and information, the basic functions of the decision support system include: 1) navigational situation analysis; 2) solving collision situations; 3) interaction with the navigator via a user/operator interface. For a system to be effective and practically used, it has to present selected information in a readable manner and to be user-friendly. In this connection, a lot of attention is paid to the issues connected with building a proper user interface. One important requirement is the compatibility with present standards of information presentation in navigational information systems[1], [2].

NAVDEC – Navigational Decision Support System

The known navigational systems in use and methods of navigational decision support perform information functions and as such are helpful in the process of safe conduct of a ship. However, none of these known systems provides a navigator with ready solutions of collision situations taking account of all the vessels in the proximity of own ship, where the Collision Regulations [3] apply. Another shortcoming of these systems is that they do not explain the assessment of a navigational situation and proposed manoeuvre parameters.

Systems presently used on ships are information systems only. NAVDEC is not only information system. It’s also decision support system.

Developed at the Maritime University of Szczecin NAVDEC system is a navigation tool that performs alongside providing information typical tasks for decision support systems. NAVDEC is an important complement to navigational equipment of the ship. Is a real-time system operated by the navigator. Its proper functioning requires interaction with devices and systems on the ship. The standard configuration of the ship include: log, gyrocompass, radar, echo sounder, ARPA, GNSS (Global Navigational Satellite System), such as GPS (Global Positioning System) or DGPS (Differential Global Positioning System). In addition, AIS, ECDIS, GNSS. In the version being developed following sources of information are in use: log, gyrocompass, radar / ARPA, GPS and DGPS, AIS and ENC (Fig.1).

Fig. 1. Data sources for decision supporting system [4]

Actual optimization in the NAVDEC system

The purpose of optimization is the choice of minimally-time manoeuvre from all available solutions, leading to pass other targets at presumed CPA (Closest Point of Approach). To achieve this goal, the following optimization criteria were used in NAVDEC: energy optimization, time optimization.

First step of the actual optimization method involves the determination of the courses leading to pass at presumed distance (Safe_Courses procedure). The courses are calculated on the basis of [5] for each pair: the own ship (number 1) and the target ship i (for i = 2 to n, where n is the number of target ship).

Input data:
- position (x1, y1), speed (V1) and course over ground (K0d1) of the own ship,
- position (xi, yi), speed (Vi) and course over ground (K0di) of target,
- CPA – safe passing distance set up by navigator.

Output data:
- Safe_Courses: <gamma1, gamma2 >, <gamma3, gamma4> - sectors of safe courses for pair: the own ship and the target ship number i.

Safe_Courses(i):

\begin{align*}
\text{zw} &= \text{xi} - \text{x1}; \quad \text{yw} = \text{yi} - \text{y1}; \quad \text{vxw} = \text{vxi} - \text{vx1}; \\
\text{vyw} &= \sqrt{\text{vxw}^2 + \text{vyw}^2}; \\
\text{vw} &= \sqrt{\text{vxw}^2 + \text{vyw}^2}; \\
\text{D} &= \sqrt{\left(\text{zw}^2 + \text{yw}^2\right)}; \\
\text{Adcpa1} &= \left(\text{zw} \cdot \text{yw} + \text{CPA} \cdot \sqrt{\text{D}^2 - \text{(CPA)}^2}\right); \\
\text{Adcpa2} &= \left(\text{zw} \cdot \text{yw} - \text{CPA} \cdot \sqrt{\text{D}^2 - \text{(CPA)}^2}\right); \\
\text{vxi} &= \text{vxi} \cdot \sin(\text{KDd2}) = \text{vxi} \cdot \cos(\text{KDdi}); \\
\text{Bdcpa1} &= \text{Adcpa1} \cdot \sqrt{\text{vy}^2}; \quad \text{Bdcpa2} = \text{Adcpa2} \cdot \sqrt{\text{vy}^2}; \\
\end{align*}
\[
\text{gamma}_1 = 2 \cdot \text{atan}((\text{Adcpa} + \text{V1} + \sqrt{(\text{Adcpa} + \text{Adcpa} + 1) \cdot \text{V1} \cdot \text{V1} - \text{Bdcpa} \cdot \text{Bdcpa}}) / (\text{Bdcpa} - \text{V1})) / \pi;
\]
\[
\text{gamma}_2 = 2 \cdot \text{atan}((\text{Adcpa} + \text{V1} - \sqrt{(\text{Adcpa} + \text{Adcpa} + 1) \cdot \text{V1} \cdot \text{V1} - \text{Bdcpa} \cdot \text{Bdcpa}}) / (\text{Bdcpa} - \text{V1})) / \pi;
\]
\[
\text{gamma}_3 = 2 \cdot \text{atan}((\text{Adcpa} + \text{V1} + \sqrt{(\text{Adcpa} + \text{Adcpa} + 2 \cdot 1) \cdot \text{V1} \cdot \text{V1} - \text{Bdcpa} \cdot \text{Bdcpa}^2}) / (\text{Bdcpa} - \text{V1})) / \pi;
\]
\[
\text{gamma}_4 = 2 \cdot \text{atan}((\text{Adcpa} + \text{V1} - \sqrt{(\text{Adcpa} + \text{Adcpa} + 2 \cdot 1) \cdot \text{V1} \cdot \text{V1} - \text{Bdcpa} \cdot \text{Bdcpa}^2}) / (\text{Bdcpa} - \text{V1})) / \pi;
\]

We assume, for simply, that we get as results exactly four angles in the above algorithm for each \( i = 2 \) to \( n \). We have to run the above Safe_Courses(\( i \)) procedure for each pair: the own ship and the target ship number \( i \) (for \( i = 2 \) to \( n \)) and as the result we get all safe sectors \(< \text{gamma}_1, \text{gamma}_2 >, < \text{gamma}_3, \text{gamma}_4 >\). Next, we execute the Common_Safe_Sectors procedure for all target ships as the angle intersections of all safe sectors \(< \text{gamma}_1, \text{gamma}_2 >, < \text{gamma}_3, \text{gamma}_4 >\) (for \( i = 2 \) to \( n \)). The details of step one can be found in [7]. Let's denote by \( \text{gamma}_i \) elements of common safe sectors.

The first phase of optimization step is energy optimization (Energy_Optimization procedure). It's lead to choose new courses, from obtained solutions, which requires the smallest deviation \( Z \) from present own ship trajectory:

**Energy_Optimization:**

\[
\{
\text{for each gamma}_i \}
\]
\[
\text{Z}_i = \text{Kd} \cdot \text{d}_1 \pm \text{gamma}_i;
\]
\[
\text{Z} = \text{min} (\text{Z}_i);
\]
\[
\text{return } Z;
\]

This way we received maximum two solutions which guarantee to pass with other targets on presumed CPA.

In this case, own ship course is 280°. As a result of calculation, we received two sectors of safe courses, which lead to pass with other targets on presumed CPA (1 Nm):
- starboard sector 335.70° – 234.59°,
- port sector 236.63° – 257.06°.

Following solutions, which requires the smallest alteration of course, were chosen:
- alter course to port by 22.93° on course 257.06°,
- alter course to starboard by 55.70° on course 335.70°.

The second step of the optimization is a time optimization (Time_Optimization procedure). At the beginning distances from present position \((X_i, Y_i)\) to the closest waypoint \((X, Y)\) through point \((X_{Sk}, Y_{Sk})\) were calculated. Point \((X_{Sk}, Y_{Sk})\) is the place, where ship alter course to the closest way-point. Course alteration is executed when TCPA is -time to closest point of approach to the farest ship equals zero. From point \((X_i, Y_i)\) to point \((X_{Sk}, Y_{Sk})\) the own ship can apply on the gamma\( _i \) courses which is chosen as results of the energy optimization. Following algorithm was used to calculate the time of the course alternation.

**Time Optimization**

\[
\text{calculate TCPA}_{ti};
\]
\[
d_i = \text{V}_i \cdot \text{TCPA}_{ti};
\]
\[
\text{for each gamma}_i;
\]
\[
X_{Sk} = d_1 \cdot \sin (\text{gamma}_i) + X_i;
\]
\[
Y_{Sk} = d_1 \cdot \cos (\text{gamma}_i) + Y_i;
\]
\[
d_2 = \sqrt{(X - X_{Sk})^2 + (Y - Y_{Sk})^2};
\]
\[
t_i = \text{TCPA}_{ti} + d_2 / \text{V}_i;
\]
\[
t = \text{min}(t_i);
\]
\[
\text{return } t;
\]

The shortest time solution is marked on Fig. 2. It fulfills safety criteria and enables the quickest attainment of the closest waypoint.

As an energy optimization, two solutions were chosen:
- alter course to port by 22.93° on course 257.06°,
- alter course to starboard by 55.70° on course 335.70°.

For both solutions times required to execute whole manoeuvre were calculated. Navigator received following advice: alter course to starboard, because total time is shorter (Fig. 2).

**Improved optimization**

The authors observe that the time optimization step, introduced in the previous section, can be improved. In actual version of this second step of the optimization, the own ship is too long on the chosen course. It is on this course as the long as TCPA – TCPA for the farest ship, will equal zero. We propose new version of the optimization which is based on the assumption that the own ship change the course to the closest way-point, at the earliest position for which TCPA is greater than zero for at most one target ship. We introduce below the algorithm for the new improved version of the time optimization procedure.

**Designations:**
- \( c_m \) – own ship course maneuver
- \( c_r \) – own ship return course
- \( \text{TCPA}_{ti} \) – TCPA for \( i \)-th target ship \((i = 2..n)\)
- \( t_p \) – time availability of targets data
**Assumptions:**
- We consider only collision situations on open waters with good visibility.
- We assume, that there is no wind and no waves.
- There is no risk of close quarters situation with each target ship.
- It's possible to generate the manoeuvre for all ships in the fourth meeting phase, the latest \[7\]
- Only course manoeuvres are possible.
- We can receive information about positions \((x_i, y_i)\), speed \((V_i)\) and course over ground \((KD_{di})\) for each ship \(i = 1..n\), after each \(t_p\) seconds (in practice \(t_p\) is equal to few seconds)
- Each target ship can change the course during the maneuver of the own ship.

**Input data:**
- position \((x_1, y_1)\), speed \((V_1)\) and course over ground \((KD_{d1})\) of the own ship,
- position \((x_i, y_i)\), speed \((V_i)\) and course over ground \((KD_{di})\) of target,
- CPA – safe passing distance set up by navigator.

**Improved_Optimization** procedure works as follows:

To the line \((1)\) we determine the new course for the own ship taking into account the energy optimization. This first part of the optimization process is not different from the current version which is realized in NAVDEC. From the line \((1)\) works the new version of the time optimization procedure. After each \(t_p\) seconds we get the actual information about each ship such as the actual position, the speed and the course. Next, we calculate the actual safe courses sectors and TCPA for each target ship and run **Common_Safe_Sectors** procedure. The most important fragment of the improved version of the time optimization algorithm is selected in the frame (begins in the \((2)\) line) We determine in this step the earliest position \((X_{Sk}, Y_{Sk})\) on the own ship trajectory defined by its course manoeuvre, for which TCPA\[i\] > 0 at most \(i = 2..n\).

**Conclusion and future work**

Implementation of new optimization method enables to reduce fuel consumption. Instead of 5558 seconds in previous option, the manoeuvres based on new method took only 5503 seconds. Instead of 38603 meters, own ship

```plaintext
\begin{align*}
\text{cm} &= \text{change KD}\_d1 \text{ with Z deviation};\\
(1) \quad t &= 0;\\
\text{for} \ (i=1 \text{ to } n) \text{ get information about: actual}(x_i, y_i), \ V_i \text{ oraz } KD_{di};\\
\text{for} \ i = 2 \text{ to } n \quad \{\\
\text{Safe_Courses}(i);\\
\text{determine TCPA}[i];\\
\}\text{ determine Common_Safe_Sectors;}
\end{align*}
```

\begin{align*}
(X_{Sr}, Y_{Sr}) &= \text{the earliest position on the own ship trajectory defined by } c_r, \\
\text{for which TCPA}[i] > 0 \text{ at most one } i = 2..n; \\
c_r &= \text{course from } (X_{Sr}, Y_{Sr}) \text{ to } (X_i, Y_i); \\
t &= t + t_p; \\
\} \text{ while (the own ship trajectory defined by } c_r \\
\text{intersects at most one domain of ships } i = 2..n; \\
\text{return } t; \\
\end{align*}

![Fig. 3a. Actual time optimization example (head on orientation). Return course c_r starts after 8 minutes](image)

![Fig. 3b. Improved time optimization example (head on orientation). Return course c_r starts after 6 minutes](image)
had to pass 38191 meters. Daily fuel consumption of medium size container ship (8.000TEU-Twenty Feet Equivalent Unit) is around 260 tons. The manoeuvre shorter by 55 seconds gave total savings of 170 liters of fuel. Taking into account that such manoeuvre is executed many times per day, fuel savings are significant.

Authors presented the concept of improved time optimization algorithm of anticollision manoeuvre. This concept involves a number of simplifications for the meeting stages, which have a place in the decision making process. In addition, implementation of the algorithm in the NAVDEC system will require taking into account the limitations of restricted area during the manoeuvre and moving away from the assumption that ships can only manoeuvre by course and not by course and speed. Besides, the key point of the proposed algorithm, selected by the frame will require the use of the heuristic method with the low time complexity. In the first step authors will attempt to apply solutions based on game control [6], genetic algorithms described in [8] and [9] or evolutionary algorithms described in [10]. Exit condition of the loop will also require the use of fast solutions in the field of computational geometry.

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