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The influence of the specifications of the elements of range of exciters voltage inverters on their spectral characteristics

Abstract. The analysis of the structural scheme of the reflectometric system exciter was carried out. We show that the basic block diagram for the construction of range of the inverter is a single ring exciter digital frequency synthesizer. The mathematical model of range of the inverter exciter provides an analysis of the structural schemes of inverter with pathogen spectral methods. These expressions of the spectral power density of the phase fluctuations allowed to take into account the effect of the circuit elements of the inverter of the pathogen on its spectral characteristics and calculate the dispersion, the average deviation of the phase in the frequency band and the mean square raid exciter output signal phase.

Streszczenie. Wykonano analizę schematu strukturalnego wzbudnicy systemu reflektometrycznego. Pokazujemy, że podstawowym schematem blokowym do budowy szeregu inwerterów jest cyfrowy syntezator częstotliwości z pojedynczą pętlą. Matematyczny model szeregu falowników przedstawia analizę schematów strukturalnych falownika za pomocą metod spektralnych patogenu. Te wyrażenia widmowej gęstości mocy fluktuacji fazowych pozwoliły uwzględnić wpływ elementów obwodu falownika patogenu na jego charakterystykę widmową i obliczyć dyspersję, średnie odchylenie fazy w paśmie częstotliwości i rms wzbudnica fazy sygnału wyjściowego. (Analiza schematu strukturalnego wzbudnicy systemu reflektometrycznego).

Keywords: direct digital synthesizers, voltage inverter, PLL, phase discriminator, power generator, VCO. **Słowa kluczowe:** bezpośrednie syntezatory cyfrowe, falownik napięcia, PLL, dyskryminator fazy, generator mocy, VCO.

Introduction

The trend of wide implementation of voltage inverters in various industries is forcing to focus on issues related to electromagnetic compatibility. For example, modern power inverters keys, especially MOSFET and IGBT with have very high switching speed, become sources of electromagnetic interference. The range of generated interference extends from the carrier frequency of the inverter (several hundreds of KHz) to radio frequency (tens of MHz). Low-frequency interferences up to 2 kHz penetrate into the supply network, high-frequency (> 10 kHz) components create a powerful radio interference [1-4].

It is known that the PLL is generally described by nonlinear differential equations [5]. The non-linear nature of the circuit, which determined by the existence of semiconductor elements (diodes, transistors, thyristors, etc.) which are part of the inverter structure chart, is the reason for generating the higher harmonics. Therefore, we carry out a research on the effects of the non-linear nature of the drivers elements, namely the research of influence of range exciters and inventers systems of phase timing on the spectral characteristics. One of the major problems which must be solved during design and production of the voltage inverter is to eliminate adverse effect of the exciter on the technical characteristics (TC) of the inverter, in particular on electromagnetic compatibility. Thereby, the development of recommendations on the choice the optimal parameter values of the phase-locked loop (PLL) of frequency synthesizer on the basis of accurate numerical analysis occurring therein is very important.

For the calculated ratios we use the method of functional expansions of Voltaire, which currently is one of the most convenient and accurate methods for analyzing non-linear dynamic systems [6, 7].

Experiment

As the main circuit of direct digital synthesizers (DDS) of range exciters (which basing on the analysis of modern element base we choose the single-ringed PLL circuit in the backward circuit which is placed a frequency divider with variable division ratio of the frequency divider with variable division factor (FDVD).

The loop consists of a voltage-controlled generator, a frequency divider with variable division ratio, phase

discriminator and low-pass filter. The frequency of a voltage-controlled generator divides and compares with a stable reference frequency. The error voltage is produced with a phase discriminator and it is used to stabilize the frequency of a voltage-controlled generator. Output frequency setting is produced with a personal computer (PC) command or from a control panel which changes the distribution ratio of a frequency divider with variable division ratio. Changing the distribution ratio of a frequency divider with variable division ratio on the synthesizer output we can get network frequencies with a step.

$$f_{CO} = N f_0 , \ f_0 = \frac{f_{or}}{M},$$

where *N* is the distribution coefficient of a frequency divider with variable division ratio; *M* denotes the distribution coefficient of a frequency divider with a fixed division factor; f_0 is the comparison frequency (a step) on the phase discriminator input.



Fig. 1. Synthesizer structure chart with the pulse-phase-locked loop (PPLL): FS - feedback section, BC - buffer cascade, VCG - voltagecontrolled generator, DFVD - a frequency divider with variable division ratio, LPF - low-pass filter, PD - phase discriminator, CC - control channel, DFDF - a frequency divider with a fixed division factor.

We will carry out a spectral characteristics analysis of the selected basic structure of the voltage range exciters of the voltage inverter. For reasoning the methodology it is necessary to find the equation describing the signal spectrum at the frequency synthesizer output from its structure chart and the elements included therein.

Pulse-phase-locked loop system can be converted on the Kotelnikov theorem basis into uninterrupted one [8]. The theorem condition can be expressed in the form of inequality: $f_n \ge f_U$, where f_n is the frequency of repetition and f_U is the transmission frequency of uninterrupted particle. It should be noted, the transition, although used in practice, but it is strict and valid only at low modulation indexes. Following the methodology proposed in [9], a generalized structure chart shown in Fig. 1 can be reduced to a linear which is equivalent to the chart of the digital phase-locked loop (Fig. 2).

The system of this type is described by the differential equation:

(1)
$$p\varphi + \frac{\Omega_{y}K(p)F(\phi)}{N} = \Delta\omega_{i},$$

where K(p) is the transfer coefficient LPF; $\Delta \omega_i$ is the initial detuning; Ω_y is the retention strip; $F(\phi)$ is the normalized characteristic of phase detector.



Fig. 2. The equivalent circuit of digital loop PLL

The difference from a typical PLL system is the presence of feedback. From is characterized by. Here is a diagram of a standard system that will simplify the analysis. Voltage creates at the output of the phase discriminator:

(2)
$$e_{PD} = \psi \left(U_{SG}, U_{DFVD}, \phi^* \right),$$

where e_{PD} is the voltage at the output of the phase detector which depended on amplitudes and instantaneous differences of phases of two compared oscillations U_{SG} and U_{DFVD} of a strong generator and a frequency divider with variable division ratio accordingly; ϕ^* is the instantaneous difference of phase oscillations at the phase discriminator input.

These values are associated with the scheme parameters by following correlations:

 $(3) U_{DFVD} = k_{DFVD}U_{VCG},$

(4)
$$\phi^* = \phi_{SG} - \frac{\phi_{VCG}}{N},$$

where U_{VCG} is the voltage amplitude of a voltage-controlled generator; k_{DFVD} - voltage transfer coefficient of DFVD; N - distribution coefficient of DFVD; ϕ_{VCG} is the instantaneous phase of oscillations of VCG; ϕ_{SG} is the instantaneous phase of oscillations of a strong generator (SG).

To simplify the analysis we use the known ratio:

- (5) $\Delta \omega^*(t) = 2\pi \Delta f^*(t),$
- (6) $\phi^*(t) = \int \Delta \omega^*(t) dt.$

In this expression:

(7)
$$\Delta \omega^*(t) = \frac{N\omega_{SG} - \omega_{VCG}}{N} = \frac{\Delta \omega(t)}{N},$$

where $\Delta \omega^*(t)$ is the instantaneous difference of frequency between VCG and some equivalent strong generator which oscillations vary with a frequency ω_{ESG} which equals to:

(8) $\omega_{ESG} = N\omega_{SG}$.

There is a linear integral relation (6) between $\phi^*(t)$ and $\omega^*(t)$, so we can write:

(9)
$$\phi^* = \frac{N\phi_{SG} = \phi_{VCG}}{N} = \frac{\phi}{N},$$

where $\phi = N\phi_{SG} - \phi_{VCG} = \phi_{ESG} - \phi_{VCG}$ is the phase of oscillations difference between VCG and equivalent SG.

Using the correlation (2)...(9) we can form an equivalent circuit of the PLL, which considerably simplifies the analysis. For this we replace a real SG to an equivalent SG. VCG frequency and phase will not change their value during the transition to equivalent PD in which the amplitude is: $U_{PCG}^* = U_{PCG}K_{DFVD}$. The output voltage of equivalent PD

will be determined with the phase difference: $\phi^* = \frac{\phi}{N}$. Then,

considering that the DFVD effect is extended to other circuit elements (SG, VCG, PD), it can be omitted. The equation for an equivalent circuit is like typical one, so:

(10)
$$p\phi + \Omega_y F\left(\frac{\phi}{N}\right) K_{LPF} = \Delta \omega_i.$$

If we talk about the complex LPF, the non-linear characteristic of PD and the control element of the equation (10) is non-linear differential equations of higher order, the exact analytical solution is associated with certain difficulties and is not currently received.

The spectral frequency of the output signal DS is determined not only with a strong generator stable but depends on the PLL ring. PLL rings influence on the stability of the output signal DS occurs in different blocks of the random phase (frequency) modulation, due to the intrinsic noise of the circuit elements.

We assume that the perturbation is small and does not derive from the state of the PLL circuit matching. Then the linearization of PLL non-linear equation near steady state is easy to obtain the following linear differential equation:

(11)
$$\phi^* + K_{LPF}\Omega_y |F'(\theta)| \phi = \omega_{VCG} - \omega_{SG},$$

where ω_{VCG} are the fluctuations in the frequency of a controlled oscillator; ω_{SG} - fluctuations in the frequency of a

power generator and
$$\theta = \arccos\left(-\frac{\Delta \omega_i}{\Omega_y}\right)$$
.

Transfer coefficient of the linear PLL has the form:

(12)
$$K(j\omega) = \frac{1}{1+G(j\omega)}, \ G(j\omega) = j\frac{K_{PD}S_{CE}K_{LPF}}{\omega},$$

where S_{CE} is the slope of the control element VCG.

The expression for the power spectral density of the phase fluctuations VCG $S_{\phi EXIT}$ we obtain through power spectral density of the phase fluctuations of free VCG and a strong generator, accordingly $S_{\phi VCG}$ and $S_{\phi SG}$:

$$S_{\phi EXIT} = S_{\phi VCG} \frac{1}{\left|1 + G(j\omega)\right|^2} + S_{\phi SG} \left|\frac{G(j\omega)}{1 + G(j\omega)}\right|^2.$$
(13)

For further analysis, we specify the type of the phase detector. We select the type of characteristics that describes:

(14)
$$F(\theta) = \cos \theta, \ \theta(t) = \theta_0 + \phi(t),$$

where $\phi(t)$ - small $\prec \phi^2 \succ \prec \prec 1$ random phase ratio.

As LPF we apply proportional-integrating filter, since it is common in these schemes, which transmission ratio has the form:

$$K_{LPF} = \frac{1 + j\omega T_1}{1 + j\omega T}, \quad (15)$$

where $T = (R + R_1)C$ i $T_1 = R_1C_1$.

By substituting (14) and (15) into (13) we obtain:

(16)
$$K(j\omega) = \frac{(1+j\omega T)j\omega}{(1+j\omega T)j\omega + \Omega_{y}(1+j\omega T_{1})\sin\theta}.$$

As it is known, the output DS wave fluctuation frequency, except for external perturbations (strong generator fluctuations) and own (fluctuations VCG) can be caused by internal noise, which together with the adjustment signal goes directly to the control element VCG. In this case, for example, for DS scheme with the converting in Fig. 3, there are additional terms in the power spectral density of the phase fluctuations of the midrange output.



Fig. 3. A structure chart of digital synthesizers of frequencies DDS with the conversion

(17)
$$S_{\phi EXIT} = S_{\phi VCG} K_1^2 (j\omega) + \left[S_{\phi SG} + S_{\phi DFVD} + S_{\phi IFA} + S_{\phi MU} \right] K_2^2 (j\omega),$$

where

$$K_{1}^{2}(j\omega) = \frac{\omega^{2}(1+\omega^{2}T^{2})}{\omega^{4}T^{4} + \omega^{2}(1+T_{1}\Omega_{y}\sin\theta_{0})^{2} - 2\omega^{2}T\Omega_{y}\sin\theta_{0} + (\Omega_{y}\sin\theta_{0})^{2}};$$

$$K_{2}^{2}(j\omega) = \frac{(\Omega\sin\theta_{0})^{2}(1+\omega^{2}T_{1}^{2})}{\omega^{4}T^{2} + \omega^{2}(1+T_{1}\Omega_{y}\sin\theta_{0})^{2} - 2\omega^{2}T\Omega_{y}\sin\theta_{0} + (\Omega_{y}\sin\theta_{0})^{2}};$$

 $S_{ASC}\phi(t)$ is the power spectral density of fluctuations in the phase of the strong generator; $S_{\rm \phi VCG}$ is the power spectral density of fluctuations in the phase of VCG; S_{øIFA} is the power spectral density of fluctuations in the phase of IFA; $S_{\phi M U}$ is the power spectral density of fluctuations in the phase of the strong generator multiplication of the frequency. The expression (17) makes it possible to take into account the effect of the synthesizer circuit elements on its output.

Results and discussion

In order to obtain the calculated ratios we use the method of functional decomposition of Voltaire and examine the equivalent model of the PLL frequency synthesizer (Fig. 2) which was gotten from a structure chart of a exciter(Fig. 1). The differential equation that describes the model can be written as [10]:

(18)
$$\dot{\phi} + \Omega_y K(p) F(\frac{\phi}{N}) = \dot{x},$$

where $\dot{\phi}$ is the difference between phases of signals of quartz and VCG generators; Ω_{y} is the retention strip; K (p) the transfer function of low-pass filter (LPF); $F\left(\frac{\phi}{N}\right) = \sin\left[\frac{\phi}{N}\right]$ is the characteristics of the phase detector; N is the division ratio of accomplice with variable division factor (DFVD) of frequency in a synthesizer; $\dot{x} = x(t)$ is the perturbations acting on the PLL circuit due to internal noise.

Following the methodology proposed in [11], we seek a solution of the equation (18) in the form of a truncated series of Voltaire:

(19)
$$\phi(t) = \sum_{n=1}^{3} \int_{-\infty}^{+\infty} d\tau_1 \dots \int_{-\infty}^{+\infty} d\tau_n h_n(\tau_1, \dots, \tau_n) \prod_{i=1}^{n} x(t-\tau_i)$$

where - $h_n(\tau_1,...,\tau_n)$ Voltaire's nuclei n-th order (*n*= 1, 2, 3) which characterizing the PLL.

We consider the phase detector characteristic as sinusoidal and expand it in a Taylor series:

(20)
$$F\left(\frac{\phi}{N}\right) = \sin\left(\frac{\phi}{N}\right) = \frac{\phi}{N} - \frac{1}{3!}\left(\frac{\phi}{N}\right)^3 + \frac{1}{5!}\left(\frac{\phi}{N}\right)^5 \dots$$

Substituting (20) into (19) and collecting terms in order in x(t) we get:

(21)
$$\left[\dot{\phi}_{1}(t) + \dot{\phi}_{2}(t) + \dot{\phi}_{3}(t)...\right] + \frac{\Omega_{y}K(p)}{N} \begin{cases} \left[\phi_{1}(t) + \phi_{2}(t) + \phi_{3}(t) + ...\right] - \\ \frac{1}{3!} \left[\phi_{1}(t) + \phi_{2}(t) + \phi_{3}(t) + ...\right] \end{cases} = x(t).$$

Equating terms with different powers on x (t) we get the following system of equations:

$$\dot{\phi}(t) + \Omega_{y}K(p) \frac{\phi_{1}(t)}{N} = x(t)$$

$$\dot{\phi}_{2}(t) + \Omega_{y}K(p) \frac{\phi_{2}(t)}{N} = 0$$

$$\dot{\phi}_{3}(t) + \Omega_{y}K(p) \frac{\phi_{3}(t)}{N} = \frac{\Omega_{y}K(p)}{3!N^{3}} \phi_{1}^{3}(t)$$

(

To find Voltaire nuclei we use the Laplace theory of multidimensional transforms. For a function of one variable a bilateral Laplace transform is given by:

$$F(p) = \int_{-\infty}^{+\infty} f(t) e^{-pt} dt, \quad f(t) = \frac{1}{2\pi j} \int_{-\infty}^{+\infty} F(p) e^{-pt} dt.$$

Similar correlations exist in the case of functions of n variables:

$$F(p_{1}...p_{n}) = \int_{-\infty}^{+\infty} dt_{1}...\int_{-\infty}^{+\infty} dt_{n}f(t_{1}...t_{n})e^{-p_{1}t_{1}-p_{2}t_{2}...-p_{n}t_{n}},$$

$$f(t_{1}...t_{n}) = \left(\frac{1}{2\pi j}\right)\int_{-\infty}^{+\infty} dp_{1}...\int_{-\infty}^{+\infty} dp_{n}F(p_{1}...p_{n})e^{p_{1}t_{1}...-p_{n}t_{n}}$$

Applying multidimensional Laplace transforms for both sides of equation (22), we get an expression for Voltaire nuclei in the operator form:

-1

$$H_{1}(p_{1}) = \left(p_{1} + \Omega_{y}K(p_{1}) \cdot \frac{1}{N}\right)^{-1},$$

$$H_{2}(p_{1}, p_{2}) = 0,$$
(23)
$$H_{3}(p_{1}, p_{2}, p_{3}) = \frac{1}{3!N^{3}} \cdot \frac{\Omega_{y}K(p_{1} + p_{2} + p_{3})}{(p_{1} + p_{2} + p_{3}) + \Omega_{y}K(p_{1} + p_{2} + p_{3}) \cdot \frac{1}{N}}$$

$$\cdot \prod_{i=1}^{3} \frac{1}{p_{i} + K(p_{i})\Omega_{y} \cdot \frac{1}{N}}.$$

Similarly, higher orders nuclei can be found. From the expressions (23) we found that the second order nucleus is 0. It can be shown that all the nuclei of paired degrees are equal to 0, in the case of odd non-linearity. Nuclei are independent of the incoming signal, they reflect the properties of the system [12]. We shall restrict our analysis to the calculation of Voltaire nuclei only the first three orders, because the nucleus of higher orders have little effect on the analysis results.

As the low-pass filter we use a proportional-integrating filter which have a transfer characteristic:

(24)
$$K(p) = \frac{mIp+1}{Tp+1}$$
,
where $T = (R_1 + R_2)C$ - filter time constant, m

Substituting (24) into the expression for the first order nucleus (22), we get an expression for the linear approximation of phase spectrum of the rigged generator:

 $\bar{R}_{1} + R_{2}$

(25)
$$S_{A}(\omega) = b^{2}\Omega_{y}^{2} \frac{\left(T + b\Omega_{y}mT\right)^{2}\omega^{2} + \left(T + b\Omega_{y}mT\right)^{2}\omega^{2} + \frac{\Omega_{y}^{2}}{\omega^{4} + \frac{1}{T^{2}}\left[1 + 2T\Omega_{y}(m-1) + m^{2}T^{2}\Omega_{y}^{2}\right]\omega^{2} + \frac{\Omega_{y}^{2}}{T^{2}}}{\left(b\Omega_{y}mT\right)^{2}\omega^{2} + \left(b\Omega_{y}\right)^{2}}.$$

We find an expression for the cubic approximation $f_0 = \omega/2\pi$ of the spectrum:

(26)
$$S_{\not A}(p_1p_2p_3) = H_3(p_1p_2p_3) \begin{bmatrix} a^3 + 3a^2bK(p_3)\Omega_y + 3ab^2K(p_2) \cdot \\ \cdot K(p_3)\Omega_y^2 + b^3\Omega_y^3K(p_1)K(p_2)K(p_3) \end{bmatrix}^3$$

Then we draw associate variables $p_1 p_2 p_3$.

It is known [13] that the spectrum of the output signal $\phi(t)$ of a non-linear dynamical system, described by a set of N Voltaire nucleus in the operator form $H_n(p_1,...,p_n)$, can be written as:

(27)
$$\Phi(p) = \sum_{n=1}^{N} \dot{A} \left\{ H_n(p_1, ..., p_n) \prod_{i=1}^n X(p_i) \right\}$$
, at $p = j\omega$

where *A* is the operator which leads to a single variable.

Combining (23) and (27) after the transition to the power spectral density of the phase fluctuations $S_{\phi}(\omega)$ we have:

$$S_{\phi}(\omega) = b^{2}\Omega_{y}^{2} \left\{ 1 + \frac{1}{3!} b^{2}\Omega_{y}^{3} \frac{K_{1}\omega^{6} + K_{2}\omega^{4} + K_{3}\omega^{2} + K_{4}}{L_{1}\omega^{8} + L_{2}\omega^{4} + L_{3}\omega^{2} + L_{4}} \right\}.$$
(28)
$$\frac{m^{2}\omega^{2} + \frac{1}{T^{2}}}{\omega^{4} + \frac{1}{T^{2}} \left[1 + 2T\Omega_{y}(m-1) + m^{2}T^{2}\Omega_{y}^{2} \right] \omega^{2} + \left(\frac{\Omega_{y}}{T} \right)^{2},$$

where $b_2[1/Hz]$ is the ratio of the noise - and the signal on power in the signal band; $m = \frac{R_1}{R_1 + R_2}$ is the proportionalintegrating factor LPF; *T* is time constant LPF.

$$\begin{split} T &= \left(R_{1} + R_{2}\right)C; \\ L_{1} &= B_{1}^{2} - 2B_{2}; \ L_{2} = B_{2}^{2} - 2B_{1}B_{3} + 2B_{4}; \ L_{3} = B_{3}^{3} - 2B_{4}B_{2}; \ L_{4} = B_{4}^{2}; \\ K_{1} &= -\left[2A_{2} + A_{1}\left(2B_{1} - A_{1}\right)\frac{b^{2}\Omega_{y}^{3}}{3!}\right]; \\ K_{2} &= 2A_{1} + 2A_{2}\left(2B_{2} + A_{2}\frac{b^{2}\Omega_{y}^{3}}{3!}\right) + A_{3}\left(2B_{1} - A_{1}\frac{b^{2}\Omega_{y}^{3}}{3!}\right) - \\ &-A_{1}\left(2B_{3} + A_{3}\frac{b^{2}\Omega_{y}^{3}}{3!}\right); \\ K_{3} &= -\left[A_{4}\left(2B_{2} - A_{2}\frac{b^{2}\Omega_{y}^{3}}{2!}\right) + A_{2}\left(2B_{4} + A\frac{b^{2}\Omega_{y}^{3}}{3!}\right) - A_{3}\left(2B_{3} + A_{3}\frac{b^{2}\Omega_{y}^{3}}{3!}\right)\right]; \\ K_{4} &= A_{4}\left[2B_{4} + A_{4}\frac{b^{2}\Omega_{y}^{3}}{3!}\right]; \\ A_{1} &= (A + C)^{3}; \\ A_{2} &= 3A^{3}\left(B + 2D\right) + 3A^{2}C\left(3D + 4B\right) + 3AC^{2}\left(5B + 4D\right) + 3C^{3}\left(2B + D\right); \\ A_{3} &= A^{3}\left(11D^{2} + 4BD + 2B^{2}\right) + 9AC^{2}\left(2B^{2} + 6BD + D^{2}\right) + \\ &+ 9AC^{2}\left(B^{2} + 6BD + 2D^{2}\right) + C^{3}\left(11B^{2} + 14BD + 2D^{2}\right); \\ A_{4} &= 3\left(A^{3}D + BC^{3}\right)\left(2B^{2} + 5BD + 2D^{2}\right) + \\ &+ 27ABCD\left[C\left(2B + D\right) + A\left(2D + B\right)\right]; \\ B_{1} &= 6\left(\frac{1}{T} + m\Omega_{y}\right); \quad B_{2} &= 11\left(\frac{1}{T} + m\Omega_{y}\right)^{2} + \frac{\Omega_{y}}{T}; \\ B_{3} &= 6\left(\frac{1}{T} + m\Omega_{y}\right)^{3} + 3D\frac{\Omega_{y}}{T}\left(\frac{1}{T} + m\Omega_{y}\right); \end{split}$$

$$\begin{split} B_4 &= 3 \left(\frac{\Omega_y}{T}\right)^2 + 18 \frac{\Omega_y}{T} \left(\frac{1}{T} + m\Omega_y\right); \\ A + C &= m; \quad BC + AD = \frac{1}{T}; \quad B + D = \frac{1}{T} + m\Omega_y; \quad BD = \frac{\Omega_y}{T}. \end{split}$$

As an example of the developed method, we carry out numerical calculations of the frequency stability of the range exciter.

To calculate the characteristics of stability, we substitute (28) into the expression for the relative value of the standard deviation of the C4 output frequency from the mean value for the measurement of time [14]:

(29)
$$\frac{\sigma[\langle \phi \rangle \tau]}{f_0} = \left(\frac{2}{\omega_0^2 \tau^2} \int_0^\infty S_p(\omega) \sin \frac{\omega \tau}{2} d\omega\right)^{\nu_2},$$

where $f_0 = \frac{\omega}{2\pi}$ - nominal output signal frequency of DS.

The calculation of the equations (28), (29) were carried out on the PC. The calculation results are shown in Fig. 4. (the solid line). The results of calculations in the linear approximation (dashed line) are also shown here. The calculations were made for a particular frequency synthesizer with parameters $b_2 = 10^{-3} Hz^{-1}$;

$$\Omega_{v} = 40 mHz$$
, $N = 20$; $m = 0.5$; $T = 1,6 \cdot 10^{-2} c$; $f_{0} = 1,15 GHz$.

Fig. 4 also shows the experimental characteristics of the midrange frequency stability of the DS (dash-dot line). The experimental and calculated points, which conducted the curves, are marked by circles. A comparison of these curves with the results of the linear theory shows a significant discrepancy (in order) of the obtained data. It should also be noted that the inclusion of non-linearity of the phase detector leads to a difference in the results only in quantitative terms, without changing mores of the dependence. Thus, the above calculations of the spectral characteristics for the non-linear model of PLL indicate that the non-linearity is necessary to be taken into account only for quantitative estimates. A simple linear model of PLL can be used to analyse the process with sufficient accuracy.



Fig. 4. Characteristics of the synthesizer frequency stability

Conclusions

The investigations have shown that the existing recommendations on the selection of parameter of range of exciters and inverters' phase synchronization systems are designed, as a rule, for linear models. This is the reason of significant differences (> 10%) between the calculated and obtained during the experimental values of the spectral characteristics.

To provide the accuracy of the estimates of the TC voltage inverters, the analysis of synchronization phase systems with the primary network of inverters, with the load and also with the pathogen-based PLL should be carried out taking into account the non-linear nature of the loop PLL-based functional method using Voltaire series. The developed calculation method allows you to get close enough (to 1%) of the experimental value estimates for both the power spectral density of the phase fluctuations, and for the discrete components of the output signal range. Any given accuracy can be obtained by selecting the required number of terms of the series.

As the basic structure of the exciter voltage inverter, the single-loop digital synthesizer based on PLL with a frequency divider in the feedback loop should be selected.

To ensure future requirements to the spectral purity of the exciter output signal, the level of side components at the output signal spectrum has to be at the background noise level (200 dB).

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