

## Research of the location of grounding conductors of electrical protection systems

**Abstract.** In the article, based on the derived equations for the smooth distribution of the flowing current along the ground electrodes of electrical protection systems, a method is proposed for calculating the service life and the permissible current load on it, which, unlike conventional calculations, does not lead to an overestimation or underestimation of the service life and the permissible load current and takes into account the method of connection cable to the ground electrode.

**Streszczenie.** W artykule, w oparciu o wyprowadzone równania na płynny rozkład przepływającego prądu wzdłuż elektrod uziemiających systemów zabezpieczeń elektrycznych, zaproponowano metodę obliczania trwałości użytkowej i dopuszczalnego na niej obciążenia prądowego, która w odróżnieniu od konwencjonalnych obliczeń, nie prowadzi do zawyżenia lub zaniżenia trwałości użytkowej i dopuszczalnego prądu obciążenia oraz uwzględnia sposób podłączenia przewodu do elektrody uziemiającej. **(Badania lokalizacji przewodów uziemiających w układach zabezpieczeń elektrycznych)**

**Key words:** electrical protection, grounding conductors, flowing current density, soil resistance.

**Słowa kluczowe:** ochrona elektryczna, przewody uziemiające, gęstość prądu płynącego, rezystancja gruntu.

### Introduction

The continuing rapid growth in the length of main and distribution oil and gas pipelines operating in zones influenced by stray currents puts one of the first places on the further development of electrical protection issues as one of the economical and promising methods.

Electrical protection measures include preserving underground metal pipelines using electrical drains, cathode installations, protectors, etc.

One of the main and important components of electrical protection against stray currents are grounding electrodes, which create a closed circuit through which current flows from the positive pole of the current source to the grounding electrode. Therefore, the choice of its design and type is largely determined by the technical and economic performance indicators of electrical protection installations. Power losses in grounding account for about 70% of the total losses [1-10].

### Principles for calculating the draining current of grounding conductors.

When calculating the service life  $T$  and permissible current load  $I_d$  of anode grounding systems of electrical protection systems of underground metal structures, certain simplifying assumptions are used. Thus, for ground electrodes located in homogeneous soil or in one of the horizontal layers of layered soil [1], it is assumed that the density of the flowing current  $j$  ("leakage current), including the dissolution current of the ground electrode, is the same along its entire length. This assumption is true in many cases [2].

For vertical grounding conductors crossing the interface between layers of layered soil [8], it is assumed that the current density  $j_i$  in each  $i$ -th layer along the length of the corresponding part  $i$  of the grounding conductor is constant and inversely proportional to the resistivity  $\rho_i$  of the soil in this layer,  $j_i \sim \rho_i^{-1}$  [3]. This assumption was also used when calculating the current spreading resistance  $R$  of such grounding electrodes in two-layer soil using the method of induced potentials, as well as when estimating the service life and permissible current load, taking into account the primary and temporary redistribution of current between the upper and lower parts of the grounding electrode due to the effect of mutual influence (shielding). However, the validity

of the above relationship is questioned by the well-known grounding equation for the distribution of the flowing current along the length in homogeneous soil, which shows that the dependence of the density of the flowing current on the resistivity of the soil is much weaker than the inverse proportionality, or is completely absent.

In addition, it is usually implicitly assumed that the method of connecting the cable to the ground electrode does not affect the service life and permissible current load values. However, preliminary estimates have already shown that they may depend on how the current is supplied - to one end of the ground electrode, to both, or between them. Such connections are further designated for brevity as one - , two - and end-to-end [7].

### Ground electrode located in homogeneous soil.

With a single-end supply of current  $I_0$  at point  $x=0$  of a grounding electrode of length  $l$ , the current distribution along it is described by the equation

$$(1) \quad I(x) = I_0 \frac{\text{sh}[\alpha(l-x)]}{\text{sh}(\alpha l)},$$

where:  $\alpha$ - is the current propagation coefficient, determined in the general case by the expression [5].

$$(2) \quad \alpha = \sqrt{r/lR} = \sqrt{\rho_a/S l R},$$

where:  $r$  - is the longitudinal resistance of the ground electrode per unit length,  $\rho_a$  is the resistivity of the anode material,  $S$ - is its cross-sectional area.

The density of the flowing current is equal to the derivative of the function  $I(x)$ .

Further, to simplify the notation and presentation, by the value  $j$  we will understand the modulus of the relative linear density of the flowing current [6,7,8]:

$$(3) \quad j(x) = \frac{1}{I_0} \left| \frac{dI(x)}{dx} \right| = \alpha \frac{\text{ch}[\alpha(l-x)]}{\text{sh}(\alpha l)}.$$

At  $l_0=1$  the value of  $j$  is equal to the linear density of the flowing current. For  $\alpha l \ll 1$ , expansion of (1) and (3) into Maclaurin series gives, respectively,

$$(4) \quad I(x) = 1 - x/l,$$

$$(5) \quad j = l^{-1}.$$

Expression (5) is the justification for the mentioned assumption about the constancy of the rate of dissolution of the ground electrode along its length. However, in the aspect considered here, it is also remarkable in that it shows the independence of  $j$  at small  $\alpha l$  from the characteristics of the ground electrode ( $\rho_a$ ,  $S$ ), soil ( $\rho$ ) and the location of the ground electrode in the ground (vertical or horizontal; from certain depths - distances  $t$  from the surface land).

Counting the second coordinate  $y$  from the end  $x=l$ , it is easy to verify that when a current of  $0,5I_0$  is supplied to each end of the ground electrode, the current distribution along its length has the form  $I(x, y) = \frac{0,5I_0}{sh(\alpha l)} \{sh[\alpha(l-x)] + sh[\alpha(l-y)]\}$

Differentiating (6) with respect to  $x$ ,  $y$  and then replacing the variables ( $y = -x$ ), for the distribution of current  $j$  we obtain the expression

$$(6) \quad j(x) = \frac{0,5\alpha}{sh(\alpha l)} \{ch[\alpha(l-x)] + ch(\alpha x)\}.$$

It is useful to introduce a correction (for calculations of  $T$  and  $I_d$ ) coefficient of uneven dissolution of the ground electrode  $k_n$ , defining  $k_n$  as the ratio of the highest current  $j$  to the value  $ac$

puted under the assumption of uniform current distribution (equation (5)). In many special situations  $k_n=1$ , but in the general case, when the inequality  $\alpha l \ll 1$  is not necessarily satisfied, the introduction of  $k_n$  allows you to calculate  $T$  and  $I_d$  based on the dissolution rate that occurs in the most dangerous zones of the ground electrode - at the cable connection points [1].

Using equations (3) and (7), we can verify that with a single-end supply of current  $I_0$  (at point  $x=0$ ) and two-end supply of currents  $0,5I_0$  (at points  $x=0$  and  $y=l$ ), the value of  $k_n$  is determined accordingly by the equations

$$(8) \quad k_{n1} = \alpha / cth(\alpha l),$$

$$(9) \quad k_{n12} = \frac{\alpha l}{2sh(\alpha l)} [ch(\alpha l) + 1],$$

that is, with a known  $\alpha$ , the value of  $k_n$  is easily calculated. This allows you to calculate the permissible amount of electricity  $Q_d$  using a simple formula

$$(10) \quad Q_d = I_d T = \frac{\varepsilon M}{E_c k_n},$$

where:  $\varepsilon$  - is the safety factor,  $M$  is the mass of the ground electrode,  $E_c$  is the empirical average (in the operating range of current densities) current consumption of the ground electrode material. Equation (9) differs from the usually used one in the presence of the coefficient  $k_n$  in the denominator and becomes normal when  $k_n = 1$ .

The dependences of the coefficients  $k_n$  on  $\alpha l$  (Fig.1) show that in all cases  $k_{n12} < k_{n1}$ , i.e. a two-ended cable connection provides a more uniform distribution of the flowing current than a single-ended one.

With increasing  $\alpha l$ , both coefficients increase. However, taking into account the low accuracy of the experimental determination of  $E_c$  and the values of  $\rho$  and  $\rho_a$  that affect  $\alpha$ , it is unlikely that serious importance should be given to an increase in  $k_n$  by less than 10-12%. It can be accepted that  $k_{n1}$  should be taken into account at  $\alpha l \geq 0,55$ , and  $k_{n12}$  - at  $\alpha l \geq 1,25$  (Fig. 1) [1,5].

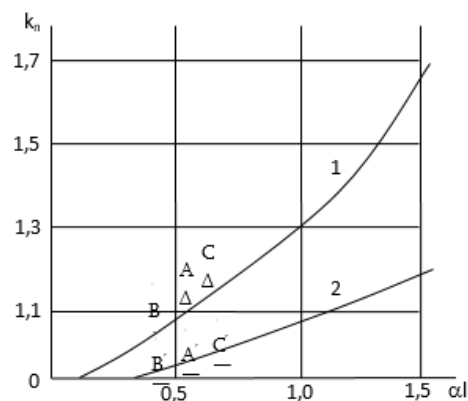


Fig.1. The influence of  $\alpha l$  on the correction factors  $k_{n1}$  (1) and  $k_{n12}$  (2) in homogeneous soil.

In connection with this, it is advisable to assess how realistic such values of  $\alpha l$  are. Table 1 shows the values of  $\alpha$  and  $\alpha l$  for some real (or similar) anode grounding conductors in soils with different resistivities [13].

For the purpose of simplification, we considered vertical non-buried ( $t=0$ ) cylindrical solid or tubular ground electrodes, for which from equation (2) and the known equations for  $R$  it follows, respectively

$$(11) \quad \alpha = \frac{2,83}{d_o} \sqrt{\frac{\rho_a}{\rho} \ln^{-1}\left(\frac{4l}{d_o}\right)};$$

$$(12) \quad \alpha = 2,83 \sqrt{\frac{1}{(d_o^2 - d_i^2)} \frac{\rho_a}{\rho} \ln^{-1}\left(\frac{4l}{d_o}\right)}.$$

where:  $d_o$  - is the outer diameter of the ground electrode,  $d_i$  - is the internal diameter of the tubular ground electrode. As can be seen from Table 1, in high-resistivity soil ( $\rho=200 \Omega \cdot m$ ) the values of  $\alpha l$  are in the range  $\approx 3 \times 10^{-3} \dots 4 \times 10^{-1}$ , i.e. and with a single-end current supply, the distribution of its flow is almost uniform ( $k_{n1} \approx 1$ ) [10].

In soil of average resistance ( $\rho=20 \Omega \cdot m$ ), the same applies to all anode grounding electrodes made of steel pipes, carbon-graphite anodes with  $l \leq 12$  m and ferrosilide №9-11. If the current supply is two-terminal, then the group in which the uneven distribution of  $j$  should be taken into account includes only grounding conductors № 8 and 13 with  $\rho = 20 \Omega \cdot m$ , and with  $\rho = 2 \Omega \cdot m$  - also №10-12. For example, for anode №11 in low-resistivity soil, the values of  $k_{n1}$  and  $k_{n12}$  are 1.8 and 1.23, i.e. the usual calculation method, allowing  $k_n=1$ , gives a value of  $T$  (or  $I_d$ ) that is overestimated by 45 and 19%, respectively [11].

Thus, the two-terminal connection expands the standard-size range of anode grounding conductors and soil resistances, where the uneven distribution of the flowing current can be neglected. It is also clear that this unevenness should most adversely affect the values of  $T$  or  $I_d$  of long anodes with relatively high  $\rho_a$  (EGT, ferrosilide), installed in low-resistivity soils and connected to the cable at only one end.

Table 1. Values of  $\alpha$  and  $\alpha l$  of some grounding conductors in homogeneous soils with different resistivities.

Number ground electrode	Anode material and shape	$d_o$	$d_i$	$l$	$\rho_a, \Omega \cdot m$	$\rho_a, \Omega \cdot m$					
						2		20		200	
						$\alpha, m^{-1}$	$\alpha l$	$\alpha, m^{-1}$	$\alpha l$	$\alpha, m^{-1}$	$\alpha l$
1	Steel, pipe	0,15	0,138	6	$1 \times 10^{-7}$	$4.8 \times 10^{-3}$	$2.9 \times 10^{-2}$	$1.52 \times 10^{-3}$	$9.2 \times 10^{-3}$	$4.8 \times 10^{-4}$	$2.9 \times 10^{-3}$
12				$4.5 \times 10^{-3}$		$5.8 \times 10^{-2}$	$1.42 \times 10^{-3}$	$1.7 \times 10^{-2}$	$4.5 \times 10^{-4}$	$5.8 \times 10^{-3}$	
60				$4 \times 10^{-3}$		0.24	$1.26 \times 10^{-3}$	$7.6 \times 10^{-2}$	$4 \times 10^{-4}$	$2.4 \times 10^{-2}$	
100				$3.83 \times 10^{-3}$		0.383	$1.21 \times 10^{-3}$	0.121	$3.83 \times 10^{-4}$	$3.83 \times 10^{-2}$	
5	Carbon graphite (EGT), Kernel	0,11	-	3	$2.22 \times 10^{-5}$	$8.7 \times 10^{-2}$	0.26	$2.75 \times 10^{-2}$	$8.2 \times 10^{-2}$	$8.7 \times 10^{-3}$	$2.6 \times 10^{-2}$
6				$8.13 \times 10^{-2}$		0.49	$2.6 \times 10^{-2}$	0.155	$8.2 \times 10^{-3}$	$5.1 \times 10^{-2}$	
12				$7.65 \times 10^{-2}$		0.92	$2.4 \times 10^{-2}$	0.29	$7.6 \times 10^{-3}$	$9.2 \times 10^{-2}$	
60				$6.8 \times 10^{-3}$		4.08	$2.15 \times 10^{-2}$	1.29	$6.8 \times 10^{-3}$	0.408	
9	Ferrosilide, kernel	0,05	-	7	$6.3 \times 10^{-5}$	0.126	0.88	$4 \times 10^{-2}$	0.278	$1.26 \times 10^{-2}$	$8.8 \times 10^{-2}$
10				14		0.12	1.656	$3.18 \times 10^{-2}$	0.524	$1.2 \times 10^{-2}$	0.166
11		0,10		28		$6 \times 10^{-2}$	1.68	$1.9 \times 10^{-2}$	0.53	$6 \times 10^{-3}$	0.168
12				60		$5.7 \times 10^{-2}$	3.42	$1.8 \times 10^{-2}$	1.08	$5.7 \times 10^{-3}$	0.34
13				50		-	-	$3.48 \times 10^{-2}$	1.744	-	-

### Grounding conductor located in one of the layers of two-layer soil.

If the grounding conductors are located entirely in one of the layers of a two-layer soil, to calculate  $\alpha$  using equation (2), the values of R found from the corresponding Burgsdorff equations should be used. Under this condition, the ground electrode can be considered as located in homogeneous soil and used to calculate  $j(x)$  of equation (1).

Due to the relative complexity of the design equations for the end-to-end cable connection, let us compare this method with those discussed above using the specific example of Fig.2, which shows the distribution of the flow of the same total current ( $I_0$ ) along the length of the ground electrode [5] in all three cases of supply. As you can see, the maximum values of  $j$  (and, naturally,  $k_n$ ) for inter-, one- and two-end cable connections are respectively 1.462: 1.141:1.000. Qualitatively the same picture was obtained in other cases. Thus, the most uneven distribution of the flowing current is created with an end-to-end connection.

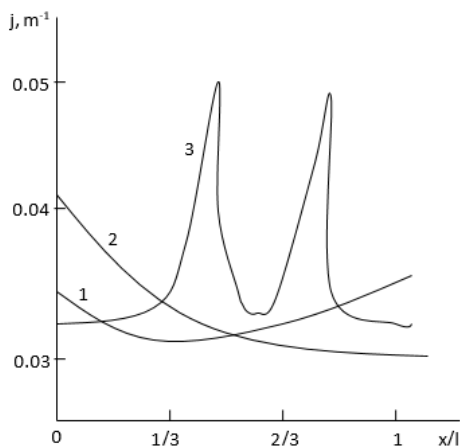


Fig.2. Dependence of the relative linear density of the flowing current  $j$  on  $x/l$  for two-end (1), single-end (2) and (3) inter-end connection of the cable to the ground electrode in homogeneous soil.

In view of the fairly widespread use of coke coating of anode grounding electrodes, it seemed useful to evaluate its effect on current distribution. A corresponding correct estimate is possible with a known specific resistance of the sprinkling  $\rho_0$ . In this case, for a ground electrode with a sprinkling of diameter  $d_0$ , under the usual assumption  $\rho_0 \ll \rho$ , the longitudinal resistance per unit length  $r$ , included

in equation (2), for example, for a tubular anode, is equal to [11,12,13]

$$(13) \quad r = \frac{1.274 \rho_a \rho_0}{\rho_a (d_0^2 - d_{ou}^2) + \rho_0 (d_{ou}^2 - d_i^2)}$$

In the design equation for R included in equation (2),  $d_0$  should be substituted instead of  $d_{outer}$ , and in equation (8) for  $Q_d$  – the value of  $E_c$  for the ground electrode with sprinkling. We have not encountered the value  $\rho_0$  in the literature.

Therefore, a quantitative assessment was carried out for anodes №1-6 of Table 1 with  $d_0=0.35m$ ,  $\rho=20 \Omega \cdot m$  and the assumption that  $\rho_0$  is 10 times greater than for solid carbon graphite, i.e. equals  $2.2 \times 10^{-4} \Omega \cdot m$ . As could be expected, for a steel grounding conductor (№ 2), for which this value is two orders of magnitude greater than  $\rho_a$ , sprinkling increases  $\alpha l$ , but only slightly – from 0.017 to 0.018, negligibly increasing the values of  $k_{n1}$  and  $k_{n12}$ , in both cases differing from one only [5,8.9] in the third and fourth decimal places. Consequently, in this case, sprinkling is useful only from the point of view of reducing the current consumption of grounding material. In all other cases, sprinkling reduced  $\alpha l$ . Although this decrease was significant (by 47-89%);  $k_{n1}$  without sprinkling exceeded 1.1 only for anodes №12 and 13 – 1.36 and 1.85, respectively. Sprinkling reduced these values to 1.105 and 1.011, i.e. ensured an almost uniform distribution of  $j(x)$ . For ground electrode №12 without sprinkling, the  $k_{n12}$  value was 1.026, i.e. we can say that in this case, uniform dissolution can be ensured either by sprinkling or by connecting the cable at two ends. For ground electrode №13, the values of  $k_{n12}$  without sprinkling were 1.24, with sprinkling -1.003, i.e. even with a double-ended cable connection, its equalizing effect was useful. Thus, with the accepted value of  $\rho_0$ , sprinkling in some cases can improve the uniformity of dissolution of ferrosilide anode grounding conductors. A decrease or increase in real  $\rho_0$  against this value, respectively, improves or worsens the leveling effect of the sprinkling. If  $\rho_0$  is unknown, then in two situations an approximate estimate is sufficient, taking into account the influence of the sprinkling only on the value of  $E_c$ . So, if (as in some of the examples given) for carbon-graphite and ferrosilide anodes  $\alpha l$  in the absence of sprinkling does not exceed 0.55 for a single-end connection and 1.25 for a double-end connection, then the improvement in the distribution of the flowing current by sprinkling practically does not matter. In the case of steel or cast iron grounding

conductors ( $\rho_a \leq 10^{-5} \Omega \cdot m$ ), the relation  $\rho_a \ll \rho_0$  is satisfied [7,9,10]. And if  $d_0$  and  $d_i$  are quantities of approximately the same order, then the first product in the denominator of the right-hand side of equation (8) can be neglected, and it takes the same form as in the absence of sprinkling:

$$(14) \quad r = \frac{1.274 \rho_a}{d_0^2 - d_i^2}.$$

In homogeneous soil, the usual calculation can overestimate, and for vertical grounding conductors crossing the interface between layers of two-layer soil, it can significantly underestimate or overestimate  $T$  or  $I_d$ . It is shown that it is advisable to calculate these quantities using the same simple formula (9) for all cases, which includes the coefficient  $k_n$ , determined by the value of  $j$  in the most dangerous zone of the ground electrode - at the cable connection point [13].

### Conclusions

The applied methods for calculating the service life  $T$  and permissible current load  $I_d$  of grounding conductors of electrical protection systems of underground metal structures are critically analyzed. It is shown that the distribution of the flowing current  $j(x)$  along the length ( $x$ ) of the ground electrode is influenced by the method of connecting the cable. The distributions  $j(x)$  are derived for a two-terminal cable connection to a ground electrode located in homogeneous soil or in a homogeneous layer of soil.

The main parameter that determines  $j(x)$  is the uneven resistance of the soil, the product  $\alpha l$  of the coefficient of propagation (spreading) of the current  $\alpha$  in the soil along the length of the grounding rod  $l$  (or its section in the soil space). The specified limit values  $\alpha l$ , above which legality is taken into account, are usually allowed for uniform distribution of the flowing current along the length of the ground electrode or its section away from the ground. It is shown that for small  $\alpha l$  (at least  $\leq 0.55$ ), a vertical ground electrode crossing the interface between layers of a two-layer soil can be considered as advancing in soil obstacles.

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