Lyapunov-Based Robust Power Controllers for a Wind Farm Using Parallel Multicell Converters

Abstract. In this paper, a robust nonlinear control technique for Wind Farm (WF) using a Doubly Fed Induction Generator (DFIG) via a parallel multicell converter (PMC) based on variable speed Wind Energy Conversion Systems (WECS) is presented. The principal concept is to use the backstepping technique to separate the DFIG’s active and reactive power rapidly. The Lyapunov function is the foundation for this control strategy, ensuring the system’s asymptotic stability. The simulation results show the implemented controller’s validity and effectiveness.

Streszczenie. W artykule przedstawiono solidną nieliniową technikę sterowania farmą wiatrową (WF) opartą na generatorze indukcyjnym z podwójnym zasilaniem (DFIG) za pośrednictwem równoległego konwertera wieloogniwnowego (PMC) stosowanego w systemach konwersji energii wiatrowej o zmiennej prędkości (WECS). Główną koncepcją jest zastosowanie techniki backstepping do solidnego rozdzielenia mocy czynnej i biełnej DFIG. Podstawą tej strategii sterowania jest funkcja Lapunowa, która zapewnia asymptotyczną stabilność systemu. Przedstawiono wyniki symulacji, aby wykazać ważność i skuteczność wdrożonego kontrolera. (Solidne sterowniki mocy oparte na Lapunowie dla farmy wiatrowej z równoległymi konwerterami wielokomórkowymi)

Keywords: Wind Farm, DFIG, parallel multicell converter (PMC), backstepping approach, Lyapunov stability.

I. Introduction

Renewable energy plays a prominent part in meeting total energy needs in the future while preserving the environment and reducing climate change. Global energy consumption has been estimated at an average yearly rate of 2%, the rest by fossil fuels [1]. With known negative effects, many countries have pushed to write challenging strategy goals for renewable energy with reduced greenhouse gas emissions and pollutant emissions, including wind energy. At the expense of the goals outlined in [2], achieving them will lead to a significant rise in the whole quantity of wind energy capacity installed in the next few decades. [3] It gives an overview of predictions for future global expansion of renewable energy sources globally. To achieve that expansion, new, massive wind farms must be planned, built, and upgraded in areas with a high potential for wind energy. Due to its partly rated power electronics converters, variable speed operation, and independent control of power, DFIG-based WF ideas are currently the most popular [4–7]. It has become imperative to improve the control of wind farms to improve energy quality through a robust control technique associated with multilevel converters. In [8] and [9], control coordinates among the wind farm, the power system, and the power load to guarantee a safe and adequate electricity flow. In [8], the backstepping control is proposed, and in [9], the predictive control is suggested. These studies rely on multilevel converters, although no attention was given to power quality in particular. [10] discusses the potential for the coordination, control, and management of various wind farm models to ensure that operational set points for active and reactive power, defined by the Spanish transmission system operator, are met. A hierarchical control structure that extends from the central control level to the control boards of each wind farm and, ultimately, to the level of each wind turbine has been used to develop and implement this coordinated control. This essay will show how both technologies (wind farms with fixed and variable speeds) can help to control the power and voltage. In [11], [12], and [13], an algorithm for power management is presented for the generation of reactive power in every wind turbine generator. The algorithm provides power reference management between the grid side converter (GSC) and the DFIG stator circuit, considering three wind farm operation modes. It also considers the maximum reactive power capability of the DFIG and the GSC. In these studies, the active and reactive power flow from the WECS to the grid is controlled with a vector control based on a conventional PI controller. In [14], [15],[16],[17],[18], and [19], the main idea is to use the backstepping method to robustly separate the active and reactive power of the DFIG in order to maintain system stability. We chose this last control technique from these studies and applied it to the wind farm due to the scarcity of research in this field. In our study, we rely on the excellent energy distribution in the wind farm that is depended on in [11], [12], considering the role of controllers and multilevel converters in improving energy quality and reducing harmonics in the farm. The article is presented as follows: power system configuration is described in section (2). The algorithm based on the proportional distribution of power references is then described in subsection (2. A). The backstepping approach of WF is summarized in detail in subsection (2. B). In subsection (2. C), we discuss modeling the parallel multicell converter (PMC). The simulations in Section 3 show the controller’s performance with the wind farm’s active and reactive power monitoring and its effectiveness in improving energy quality. Section 4 presents a conclusion.

II. Power system configuration

The grid control forces the operating center to treat the wind farm as a conventional turbine. The study’s power system contains four 1.5MW DFIG units connected to the 30kV grid via a 30kV/690V transformer, as shown in figure 1: The WF is based on the DFIG model, as detailed in [16].

Abdelkader ACHAR1*, Youcef DJERIRI1, Abderrahim BENTAALLAH1, Salah HANAFI1, Mohammed Abdeldjalil DJEHAF2, Riyadh BOUDDOU2

Department of Electrotechnics, Faculty of Electrical Engineering/Intelligent Control and Electrical Power Systems Laboratory, Djillali Liabes University, Sidi Bel-Abbes, Algeria (1)

Department of Technology, Institute of Science and Technology, University Center of Naama, Algeria (2)

ORCID: 1. 0000-0002-9756-5352; 2. 0000-0001-7590-8492; 3. 0000-0001-7982-2346; 4. 0000-0003-3089-7368; 5. 0000-0002-4482-6918; 6. 0000-0001-6555-5785

II.1 Proportional power reference distribution-based algorithm

The proportional distribution-based algorithm was created to proportionally distribute the power instructions to the wind turbines on the farm. The advantage of this strategy is that it ensures that all wind farm turbines operate far away from their maximal production capacity. There is, therefore, no risk of turbine saturation. Although one of the turbines is fully loaded, i.e., the turbine is operating at its maximal production or consumption of the

II.2 Backstepping controllers design

Designing the WF backstepping controller can be done in 2 steps [20]:

A. Active Power Control

The active power error is calculated as:

\[ e_i = P_{WG,i}^{ref} - P_{i,i} \]

With \( n \) is the DFIG number used on the farm. The derivative of (1) is:

\[ \dot{e}_i = \dot{P}_{WG,i}^{ref} - \dot{P}_{i,i} \]

Taking \( V \) as a Lyapunov candidate function:

\[ V(e_i) = \frac{1}{2} e_i^2 \]

The derivative of (3) is given by:
Substituting the power relationship \([16]\) in (4), we get:
\[
\begin{align*}
\dot{V}(e_i) &= e_i \ddot{e}_i = e_i \left( P_{WG_{i-1}} - P_{s_{i-1}} \right) \\
&\vdots \\
\dot{V}(e_n) &= e_n \ddot{e}_n = e_n \left( P_{WG_{n-1}} - P_{s_{n-1}} \right)
\end{align*}
\]

Equation (5) becomes, after substituting the derivative:
\[
\begin{align*}
\dot{V}(e_i) &= e_i \left( P_{WG_{i-1}} + \frac{3 L_m}{2 L_s} V_s (g_i \omega, 1) \right) \\
&\vdots \\
\dot{V}(e_n) &= e_n \left( P_{WG_{n-1}} + \frac{3 L_m}{2 L_s} V_s (g_n \omega, 1) \right)
\end{align*}
\]

where \(\sigma = 1 - (L_m^2 / L_s^2)\) is the leakage factor, and \(g\) is the slippage of the inductor machine. Lastly, the active power stabilizing control law is given by:
\[
\begin{align*}
V_{e_{i-1}} &= \frac{2 \sigma L_s}{3 L_m^2} \ddot{V}_{e_{i-1}} + g_i \omega \sigma L_s I_{d_{i-1}} + \frac{R}{L_s} I_{q_{i-1}} V_s (g_i \omega, 1) + \frac{2 \sigma L_s}{3 L_m^2} L_s K_i e_i \\
&\vdots \\
V_{e_{n-1}} &= \frac{2 \sigma L_s}{3 L_m^2} \ddot{V}_{e_{n-1}} + g_n \omega \sigma L_s I_{d_{n-1}} + \frac{R}{L_s} I_{q_{n-1}} V_s (g_n \omega, 1) + \frac{2 \sigma L_s}{3 L_m^2} L_s K_i e_i
\end{align*}
\]

In order to guarantee the convergence of the Lyapunov candidate function, we replace the expression (7) in (6) and obtain:
\[
\begin{align*}
\dot{V}(e_i) &= -k_1 e_i^2 < 0 \\
&\vdots \\
\dot{V}(e_n) &= -k_n e_n^2 < 0
\end{align*}
\]

Where \(k_{1-n}\) is a positive constant.

B. Control of reactive power

The error of reactive power can be given by:
\[
\begin{align*}
\dot{e}_{a1} &= Q_{WG_{1-1}} - Q_{s_{1-1}} \\
&\vdots \\
\dot{e}_{2n} &= Q_{WG_{n-1}} - Q_{s_{n-1}}
\end{align*}
\]

The derivative of (9) is:
\[
\begin{align*}
\dot{V}(e_{a1}) &= \frac{1}{2} e_{a1}^2 \\
&\vdots \\
\dot{V}(e_{2n}) &= \frac{1}{2} e_{2n}^2
\end{align*}
\]

Substituting the power relationship [28] in (12), we get:
\[
\begin{align*}
\dot{V}(e_{a1}) &= e_{a1} \ddot{e}_{a1} = e_{a1} \left( Q_{WG_{1-1}} + \frac{3 L_m}{2 L_s} V_s V_s (g_i \omega, 1) \right) \\
&\vdots \\
\dot{V}(e_{2n}) &= e_{2n} \ddot{e}_{2n} = e_{2n} \left( Q_{WG_{n-1}} + \frac{3 L_m}{2 L_s} V_s V_s (g_n \omega, 1) \right)
\end{align*}
\]

Lastly, the stabilization law of control for active power is defined by:
\[
\begin{align*}
\dot{V}(e_i) &= -k_1 e_i^2 < 0 \\
&\vdots \\
\dot{V}(e_n) &= -k_n e_n^2 < 0
\end{align*}
\]
To ensure the convergence of the Lyapunov candidate function, replacing expression (15) in (14) gives:

\[
\dot{V}(e_{n+1}) = -k_{n+1}e_{n+1}^2 < 0
\]

\[
\dot{V}(e_{2n}) = -k_{2n}e_{2n}^2 < 0
\]

Where \(k_{n+1-2n}\) is a positive constant.

II.3 Modelling of the parallel multicell converter (PMC):

The parallel multicell converter appeared in the early 1990s. This framework comprises an association of switching cells (P) interconnected via independent inductors, also called link inductors. This topology makes it possible to reduce the current constraints on the power electronics switches because each cell is under a constraint equal to \(I_E/\)P one since the cells are connected in parallel. Figure 3 shows a parallel multicell converter of P switching cells [21,22].

![Fig.3. Parallel multicell converter with P switching cells](image)

The work in this paper was done with the parallel multicell converter of 4 (P=4) switching cells and is modelled as follows:

Since we know the value of the inductance, we can obtain the equation governing the evolution of the current:

\[
L_i \frac{d}{dt} I_{i_L} = -R_{i_L} L_i I_{i_L} + V_{i_L}
\]

With: \(i = 1\) to 4. The voltage \(V_{i_L}\) is a function of the control signal of the switches \(S_i\).

This gives a new expression for the evolution of the current \(I_{i_L}\):

\[
\frac{d}{dt} I_{i_L} = \frac{-R_{i_L} I_{i_L} + S_i (E/2) - V_{i_L}}{L_i}
\]

The evolution of currents \(I_{i_L}\) is governed by equation (19). Thus, the system of equations representing the model at instantaneous values of a parallel multicell arm with four cells operating as an inverter, associated with an R-L load, is:

\[
\frac{d}{dt} \begin{bmatrix} I_{i_L} \\ I_{i_L} \\ I_{i_L} \\ I_{i_L} \\ V_s \end{bmatrix} = \begin{bmatrix} \frac{-R_{i_L} I_{i_L} + S_i (E/2) - V_{i_L}}{L_i} \\ \vdots \\ \frac{-R_{i_L} I_{i_L} + S_i (E/2) - V_{i_L}}{L_i} \\ \frac{-R_{i_L} I_{i_L} + S_i (E/2) - V_{i_L}}{L_i} \\ \frac{-V_s}{L_{ch} R_{ch}} \end{bmatrix}
\]

Let us recall the expression of the equation of state with the new matrices:

\[
\dot{X} = A \cdot X + B \cdot S
\]

With:

\[
X = [I_{i_L} \quad I_{i_L} \quad I_{i_L} \quad I_{i_L} \quad V_s]^T
\]

\[
S = [S_1 \quad S_2 \quad S_3 \quad S_4]^T
\]

\[
A = \begin{bmatrix}
\frac{-R_{i_L}}{L_i} & 0 & 0 & 0 & -\frac{1}{L_i} \\
0 & \frac{-R_{i_L}}{L_2} & 0 & 0 & -\frac{1}{L_2} \\
0 & 0 & \frac{-R_{i_L}}{L_3} & 0 & -\frac{1}{L_3} \\
0 & 0 & 0 & \frac{R_{i_L}}{L_4} & -\frac{1}{L_4} \\
1 & -S_1 & 1 & -S_2 & 1 & -S_3 & 1 & -S_4 & -\frac{1}{L_{ch} R_{ch}}
\end{bmatrix}
\]

\[
B = \begin{bmatrix}
E_1 \\
E_2 \\
E_3 \\
E_4 \\
\frac{I_{i_L}}{L_{ch}} \\
\frac{I_{i_L}}{L_{ch}} \\
\frac{I_{i_L}}{L_{ch}} \\
\frac{I_{i_L}}{L_{ch}} \\
\frac{I_{i_L}}{L_{ch}} \\
\frac{I_{i_L}}{L_{ch}}
\end{bmatrix}
\]

Where: \(E_i = E/2\)
III. Simulation results and discussion

The general structure of the proposed wind farm is based on DFIGs powered by parallel multicell converters connected to the power system, as illustrated in Figure 1. This wind farm comprises four generators (DFIG) with the same nominal power of 1.5 MW, the parameters given in the appendix are subjected to four different wind profiles. The backstepping command carries out the control of the multicell converters.

A varied wind speed operates the WF with a mean value of 8.2 m/s (Figure 4). The MPPT (Maximum Power Point Tracking) strategy generates the active and the reactive power references are maintained as steps. The proportional distribution algorithm ensures the distribution of the reference powers. This production system (wind farm and its central supervision unit) was simulated using MATLAB. Figures 5 (a, b, c, d, e, f, g, h, i, j) show centralized power supervision simulation results in a farm based on a grid operator plan. The farm is operated on an active (Fig.5. a) and reactive (Fig.5. b) power plan imposed by the network manager. This power is distributed in a weighted manner over the three wind turbines (Fig.5.c, d, e, f, g, h, i, j), which shows the application of the proportional distribution algorithm for centralized power supervision in the farm. At t = 2.5s, a third wind turbine disconnection occurred, leading to its production cancellation (Fig.5. g and h). On the other hand, the powers produced by the farm always follow their references (Fig.5. a and b). This is because the other two wind turbines generate more power to fill the power gap.

Fig.4. Wind speed profiles for each wind turbine

Fig.(5.a). Active power of the farm (reference and simulated)

Fig.(5.b). Reactive power of the farm (reference and simulated and maximum)

Fig.(5.c). Active power of the first wind turbine (reference and simulated)

Fig.(5.d). Reactive power of the first wind turbine (reference and simulated and maximum)
Fig. (5.e). Active power of the second wind turbine (reference and simulated).

Fig. (5.f). Reactive power of the second wind turbine (reference and simulated and maximum).

Fig. (5.g). Active power of the third wind turbine (reference and simulated).

Fig. (5.h). Reactive power of the third wind turbine (reference and simulated and maximum).

Fig. (5.i). Active power of the fourth wind turbine (reference and simulated).

Fig. (5.j). Reactive power of the fourth wind turbine (reference and simulated and maximum).

The THD of the farm electrical current is measured to demonstrate the parallel multicell converter's effectiveness. To do this, a constant speed is imposed on the wind farm and measured by FFT (Fast Fourier Transformation) analysis, as shown in figure 6.
The proportional distribution algorithm is applied to the central supervision of powers over the operation by deducing the following:

- According to the references imposed by the network operator, perfect control of the active and reactive power, thanks to the backstepping control application.
- All the wind turbines participate, according to the proportional distribution algorithm, in the optimal management of the active and reactive powers of the farm.
- Consideration of the maximum reactive power production capacity of every wind turbine.
- Furthermore, finally, the power quality improved at a low THD thanks to the PMC.

IV. Conclusion

This paper proposes a new topology using parallel multiscroll converters well adapted to wind farms. Then, a mechanism for managing the active and reactive power of the wind farm connected to the power system is exposed. The centralized supervision of active and reactive powers is based on the proportional distribution algorithm. The proportional distribution algorithm requires estimating the aerodynamic power of every wind turbine; thus, it ensures the operation of the latter without saturation because their power references are defined by taking into account their maximum production capacity. Indeed, it attributes the highest power references to wind turbines with the largest production capacity. Based on specific requests from the grid manager, the central supervision unit distributes the power references for each local supervision unit inside each wind turbine. The supervision algorithm is applied for managing active and reactive power and distributes the references sent by the system operator proportionally. The proportional distribution strategy ensures that each wind turbine works far enough away from its maximum energy production capacity (away from saturation). Backstepping control is offered by integrating all types of active and reactive powers from the farm. With the proposed strategy, the power management was done with excellent performance and with a very high quality of energy transmitted as well as an increase in the total yield of the wind farm.

Appendix

Table 1. presents the parameters of the DFIG used in the study. Table 2 presents the wind turbine parameters.

### Table 1. Parameters of DFIG [23]

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>Rated power, $P_n$</td>
<td>1.5 MW</td>
</tr>
<tr>
<td>Nominal wind speed, $v$</td>
<td>12.5 m/s</td>
</tr>
<tr>
<td>Stator rated voltage, $V_s$</td>
<td>398/690 V</td>
</tr>
<tr>
<td>Stator rated current, $I_n$</td>
<td>1900 A</td>
</tr>
<tr>
<td>Stator rated frequency, $f$</td>
<td>50 Hz</td>
</tr>
<tr>
<td>Stator inductance, $L_s$</td>
<td>0.0137 H</td>
</tr>
<tr>
<td>Rotor inductance, $L_r$</td>
<td>0.0136 H</td>
</tr>
<tr>
<td>Mutual inductance, $M$</td>
<td>0.0135 H</td>
</tr>
<tr>
<td>Stator resistance, $R_s$</td>
<td>0.012 Ω</td>
</tr>
<tr>
<td>Rotor resistance, $R_r$</td>
<td>0.021 Ω</td>
</tr>
<tr>
<td>Number of pairs of poles, $p$</td>
<td>2</td>
</tr>
<tr>
<td>Total inertia $J$</td>
<td>1000kg.m²</td>
</tr>
</tbody>
</table>

### Table 2. Wind turbine parameters [23]

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>Number of blades</td>
<td>3</td>
</tr>
<tr>
<td>The radius of the rotor $R$</td>
<td>35.25 m</td>
</tr>
<tr>
<td>Speed multiplier gain $G$</td>
<td>90</td>
</tr>
<tr>
<td>Total moment of inertia $I_t$</td>
<td>1000 Kg.m²</td>
</tr>
<tr>
<td>Viscous friction coefficient $f_v$</td>
<td>0.0024N.m.s⁻¹</td>
</tr>
<tr>
<td>Starting wind speed $V_s$</td>
<td>4m/s</td>
</tr>
<tr>
<td>Stopping wind speed $V_n$</td>
<td>25m/s</td>
</tr>
</tbody>
</table>

**Authors**

Mr. Abdelkader ACHAR, Department of Electrotechnics, Faculty of Electrical Engineering/Intelligent Control and Electrical Power Systems Laboratory, Djillali Liabes University, Sidi Bel-Abbes, Algeria, E-mail: abdelkader.achar@univ-sba.dz.

Dr. Youcef DJERIRI, Department of Electrotechnics, Faculty of Electrical Engineering/Intelligent Control and Electrical Power Systems Laboratory, Djillali Liabes University, Sidi Bel-Abbes, Algeria, E-mail: youcef.djerri@univ-sba.dz.

Prof. Abderrahim BENTAALLAH, Department of Electrotechnics, Faculty of Electrical Engineering/Intelligent Control and Electrical Power Systems Laboratory, Djillali Liabes University, Sidi Bel-Abbes, Algeria, E-mail: abderrahim.bentaallah@univ-sba.dz.

Dr. Salah HANAFI, Department of Electrotechnics, Faculty of Electrical Engineering/Intelligent Control and Electrical Power Systems Laboratory, Djillali Liabes University, Sidi Bel-Abbes, Algeria, E-mail: salah.hanafi@univ-sab.dz.

Dr. Mohammed Abdeljalili DEJHAF, Department of Electrotechnics, Faculty of Electrical Engineering/Intelligent Control and Electrical Power Systems Laboratory, Djillali Liabes University, Sidi Bel-Abbes, Algeria, E-mail: med_dejha@yahoo.com

Dr. Riyadh BOUDDOU, Department of Electrotechnics, Faculty of Electrical Engineering/RECOM Laboratory, Djillali Liabes University, Sidi Bel-Abbes, Algeria, Department of Technology, Institute of Science and Technology, University Center of Naama, IEEE Member, Algeria. E-mail: ryadh.bouddou@ieee.org

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